

# NUMERICAL AND EXPERIMENTAL MODELLING OF PIEZOCONE PENETRATION IN PARTIALLY DRAINED CONDITIONS: PRELIMINARY RESULTS

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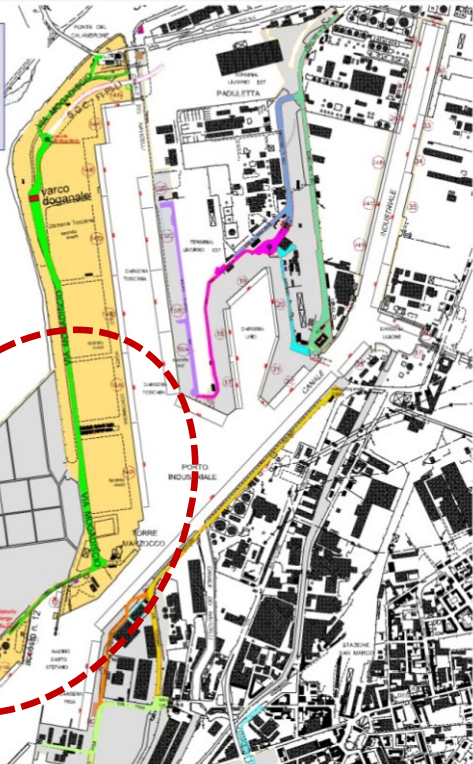
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# Livorno Port Authority



**A** Autorità Portuale  
Livorno  
DIPARTIMENTO SICUREZZA E  
CONTROLLI AMBIENTALI  
Viale della pubblica porta Livorno  
nuova leonormannaia di delbene  
Comune di Livorno n.135/2009



Artificial basin for the storage of dredged sediments (surface of 40 hectares and capacity of 1.700.000 m<sup>3</sup>); New artificial basin (35 hectares) is under design

Great interest in re-using the top surfaces of these basins for the development of Port Infrastructures

The basin is impermeable therefore dredged sediments are “underconsolidated”



Huge investigation area - it is necessary to use economic, expeditious and reliable methods to identify the soil types and their spatial variability.



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“Numerical and experimental modelling for piezocone penetration under partially drained conditions: preliminary results”

# Studies of partially drained penetration

CLAY SOILS Fully undrained conditions

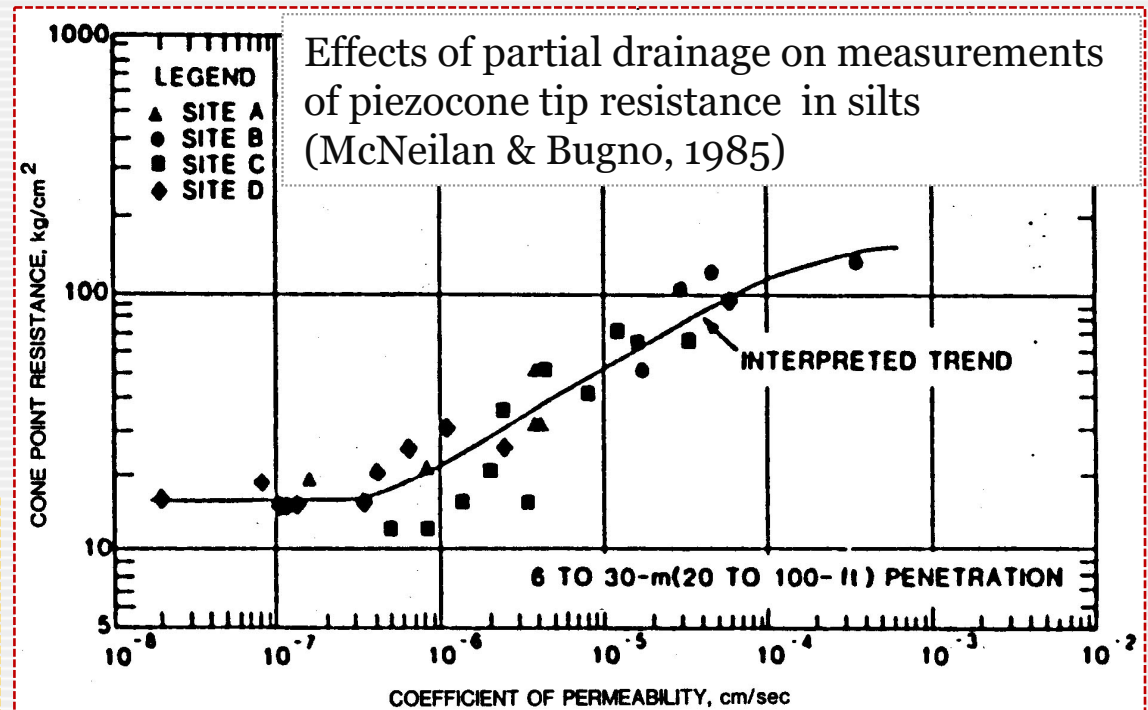
SANDS Fully drained conditions

INTERMEDIATE SOILS  
Partially drained conditions

Semi-empirical correlations

Shear strength, consolidation and permeability properties (Wroth, 1984; Baligh, 1986a, b; Teh & Houlsby, 1991)

More difficult to interpret tests results (Ramsey, 2010; Lo Presti et al., 2010)



# Studies of partially drained penetration



THE INFLUENCE OF PENETRATION RATE ON CONE RESISTANCE IS WELL RECOGNIZED:

Link between penetration resistance and the coefficient of consolidation of the soil (Randolph&Hope,2004)

## Validation

Controlled laboratory physical model tests on kaolin clay

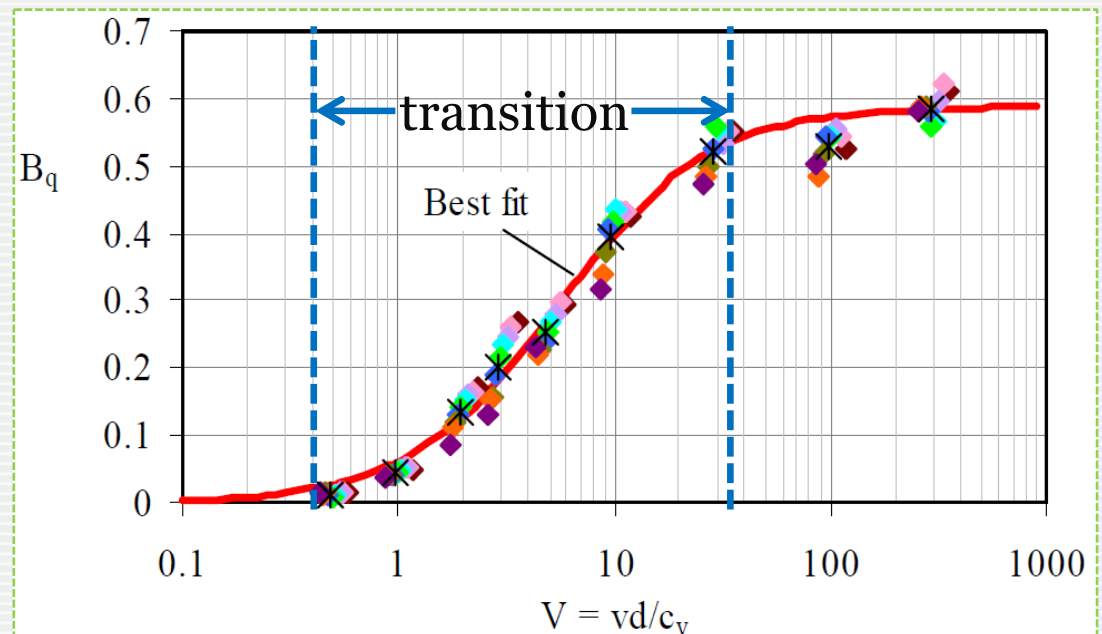
Limited number of in situ tests

(Chung et al., 2006; Lo Presti et al., 2010; Tonni et al. 2010)

T-bar penetrometer



Cylinder:  
d: 5mm  
L: 20 mm



# Studies of partially drained penetration

Randolph & Hope, 2004

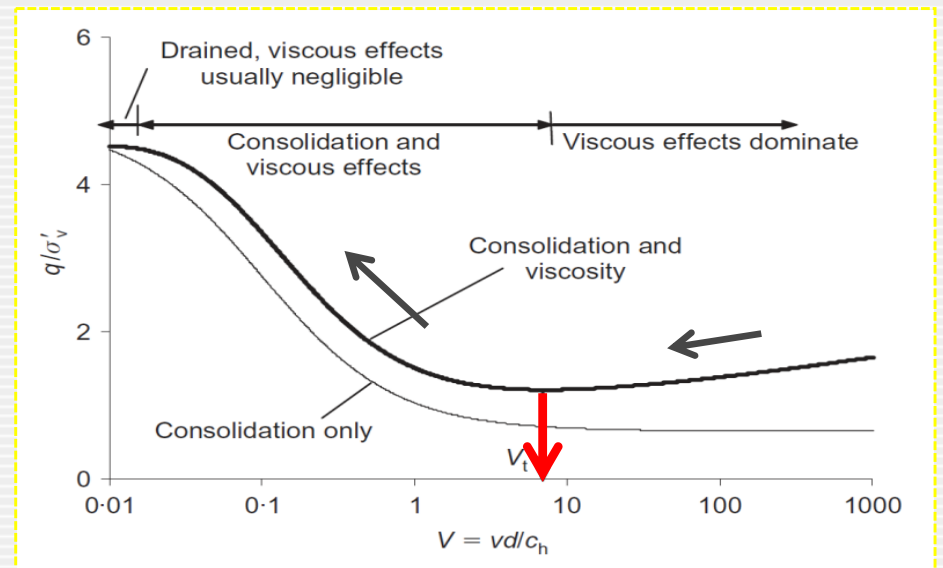
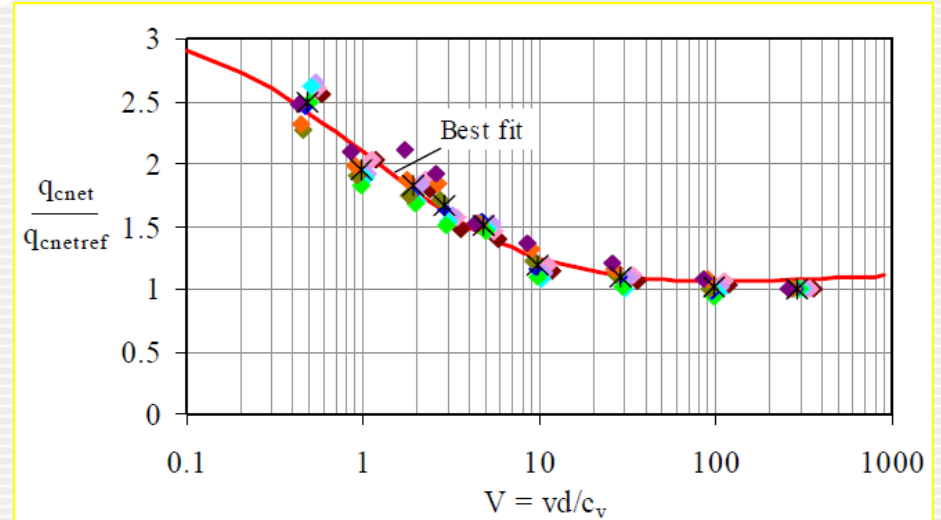
$$\frac{q}{\sigma'_v} = \left[ a + \frac{b}{1 + cV} \right]$$

Lehane et al., 2009

$$\frac{q}{\sigma'_v} = \left[ a + \frac{b}{1 + cV} \right] \left[ \frac{v/d}{(v/d)_{ref}} \right]^m$$

$$V_t \approx \left[ \frac{b}{acm} \right], m < 0.1$$

$$\left[ \frac{q}{\sigma'_v} \right]_{max, drained} = [a + b]$$



# Numerical analysis of the cone penetration process



Numerical analysis of the cone penetration process has been conducted using:

the strain path method

- (Levadoux and Baligh, 1980; Teh and Houlsby, 1991)

cavity expansion analysis

- (Vesic, 1972; Salgado et al. 1997; Yu, 2004)

finite element analysis

finite difference analysis

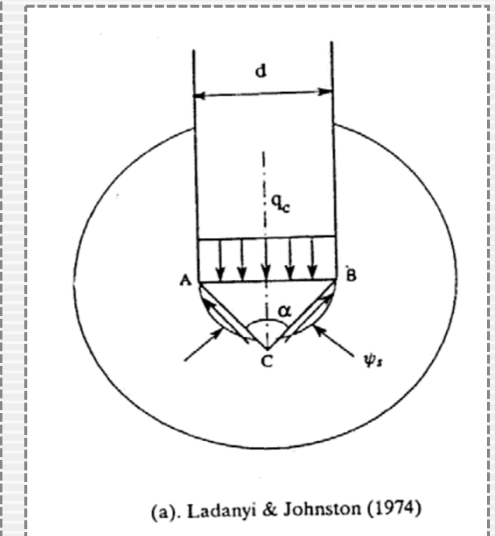
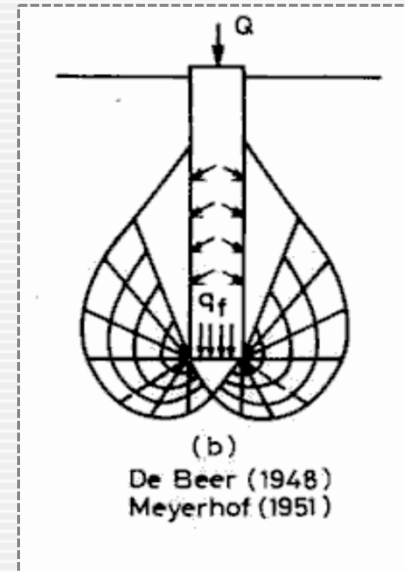
However most of these analyses assumed either **fully drained** or **undrained** conditions.

The effect of consolidation is still not well studied.



# Strain Path Method (Baligh, 1985)

BEARING CAPACITY  
AND  
CAVITY EXPANSION THEORY TREAT  
CONE RESISTANCE AS A  
COLLAPSE LOAD  
PROBLEM



Strain Path Method is the first example of **steady state approach**:  
Penetration process is treated as a **steady flow of soil** passing the **fixed cone penetrometer**

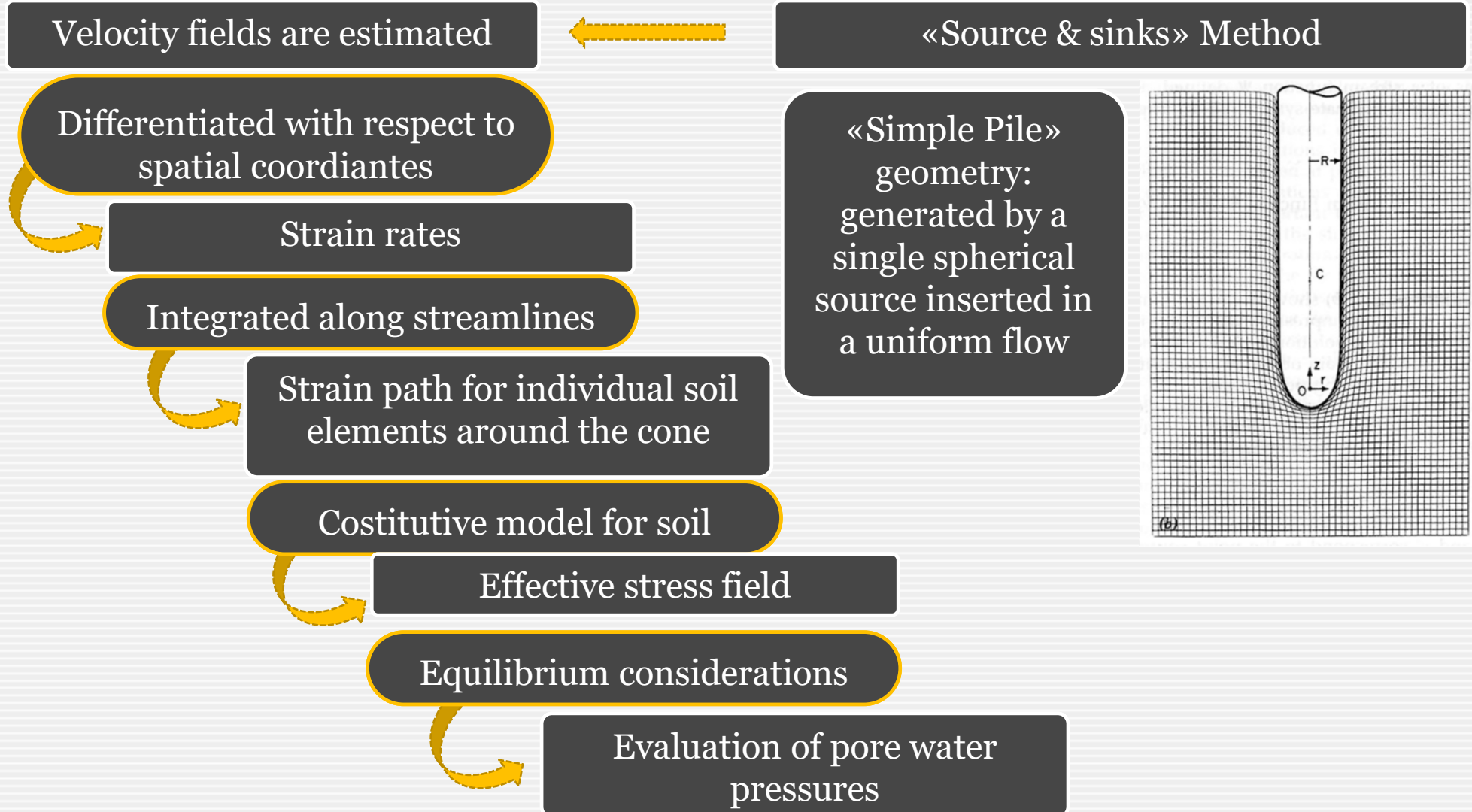
Due to the severe kinematic constraints that exist in deep penetration problems



Soil deformation are independent of shearing resistance of the soil  
Deep penetration problem is considered strain-controlled

# Strain Path Method (Baligh, 1985)

Deep undrained penetration:





# Strain Path Method (Baligh, 1985)

DISTINCT MODES OF SHEARING CAN BE DEFINED

Segment A:  
Principal mode of shearing is triaxial compression

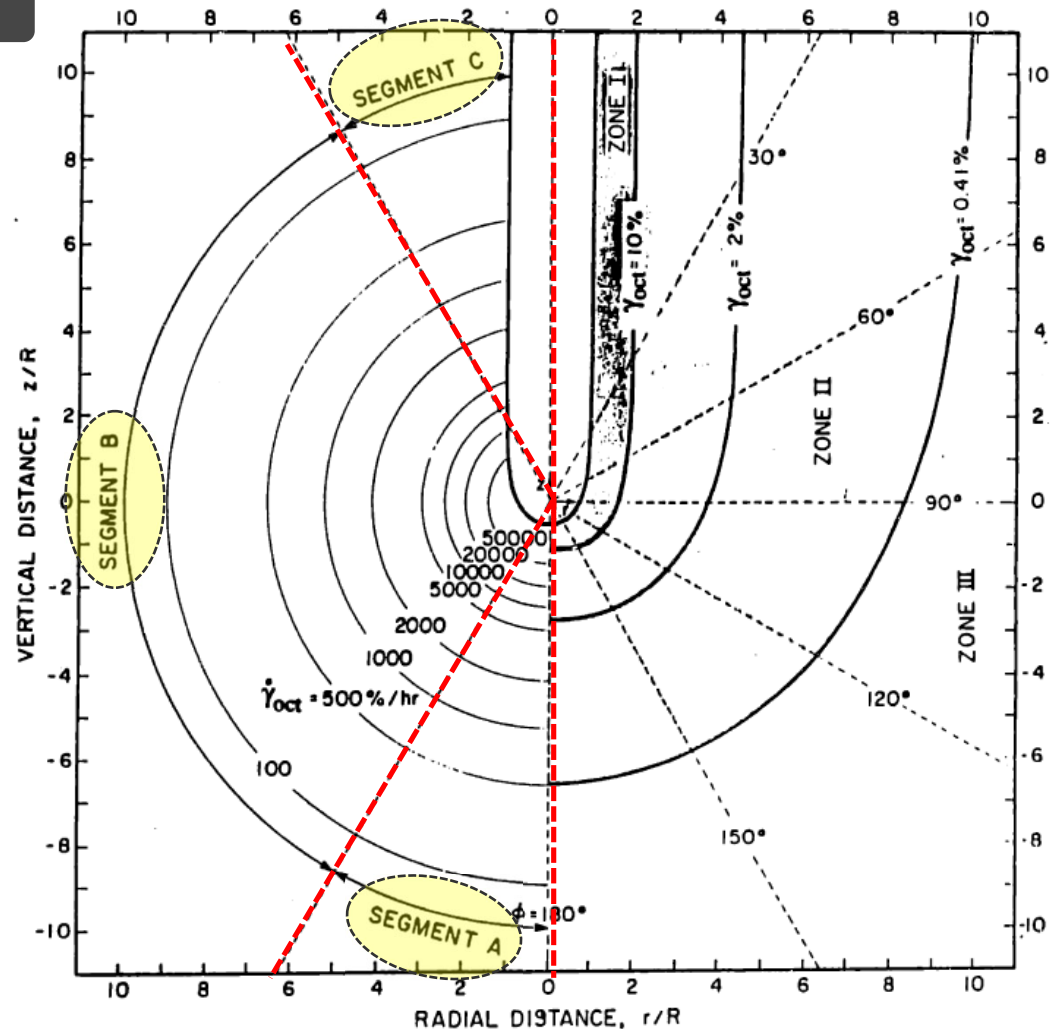
Segment B:  
Rotation of principal strain directions & reversal of individual strain components

Segment C: conditions similar to the expansion of a cylindrical cavity

The complete analysis of the simple pile geometry using the SPM is highly complex

$R = 1.78 \text{ cm}$ ,  $U = 2 \text{ cm/s}$

Octahedral strain rates contour



Octahedral strain contour

# Strain Path Method (Baligh, 1985)

**Elghaib (1989)** developed a simplified predictive framework based on the SPM for conditions along the centerline of the simple pile penetrometer

- The mode of shearing of soil elements is restricted to triaxial compression
- Monotonically increasing strain rates and strain components magnitudes
- Small gradients of the field variables in the radial direction - conditions of vertical equilibrium

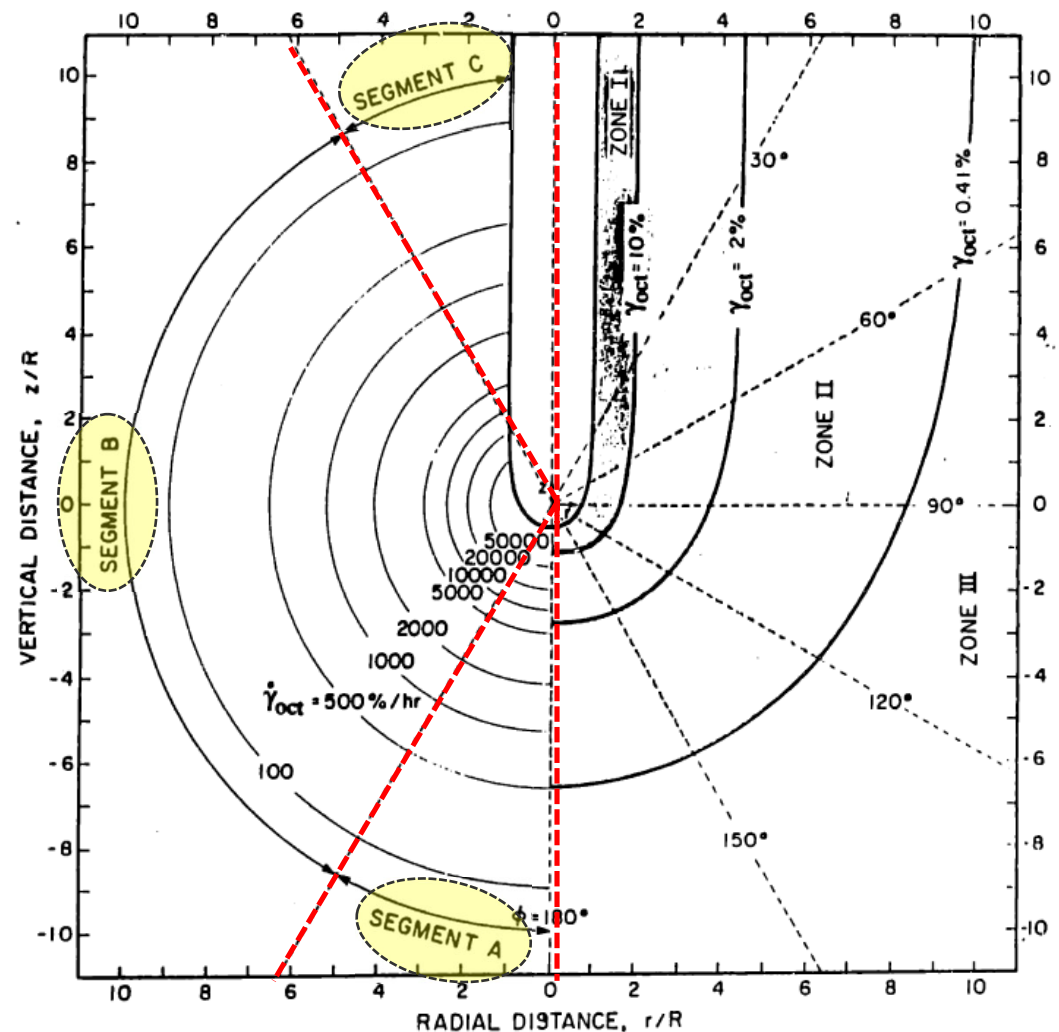


Closed form solutions along the centerline for the simple pile geometry

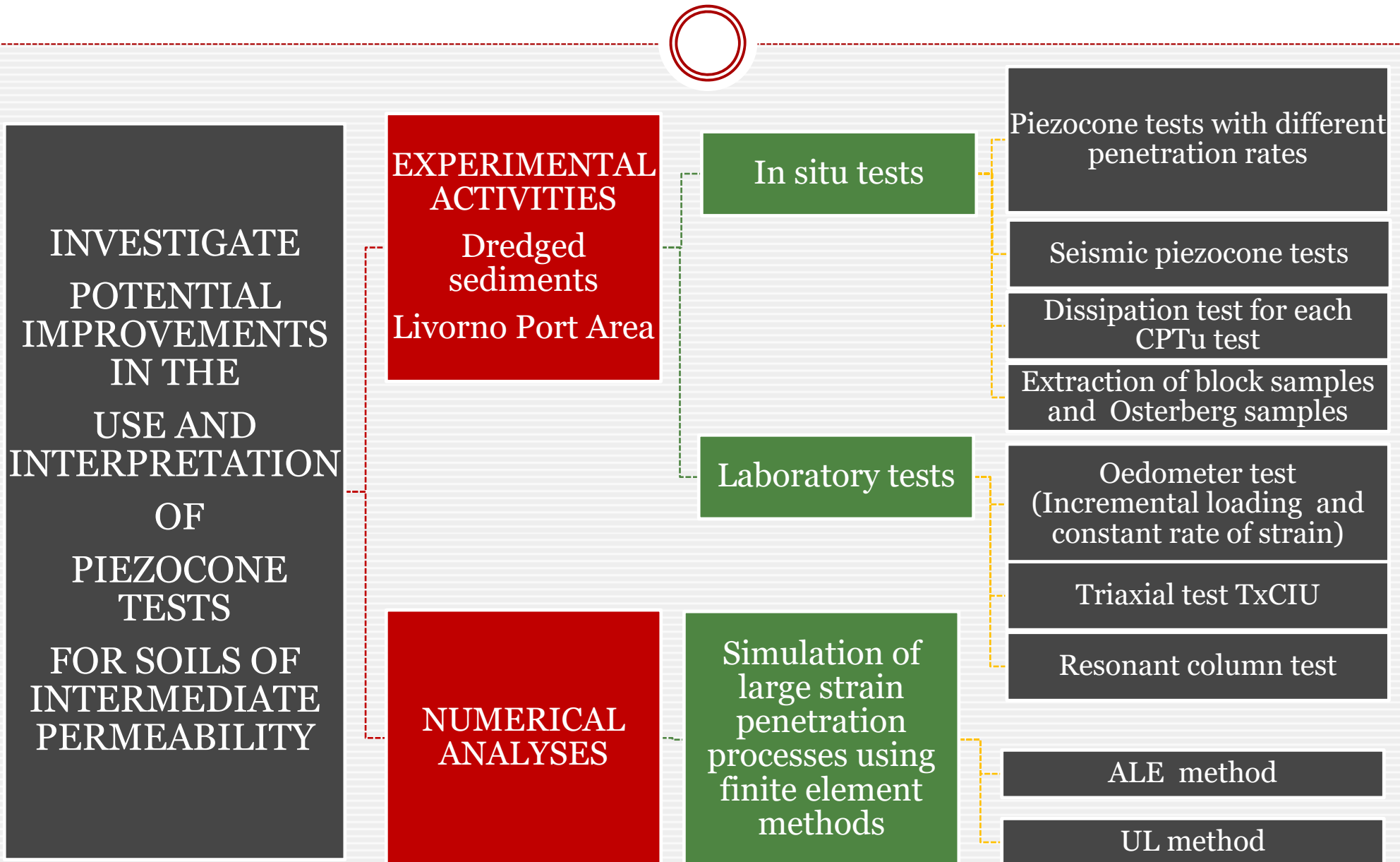
Permits partial drainage to be incorporated in the analysis



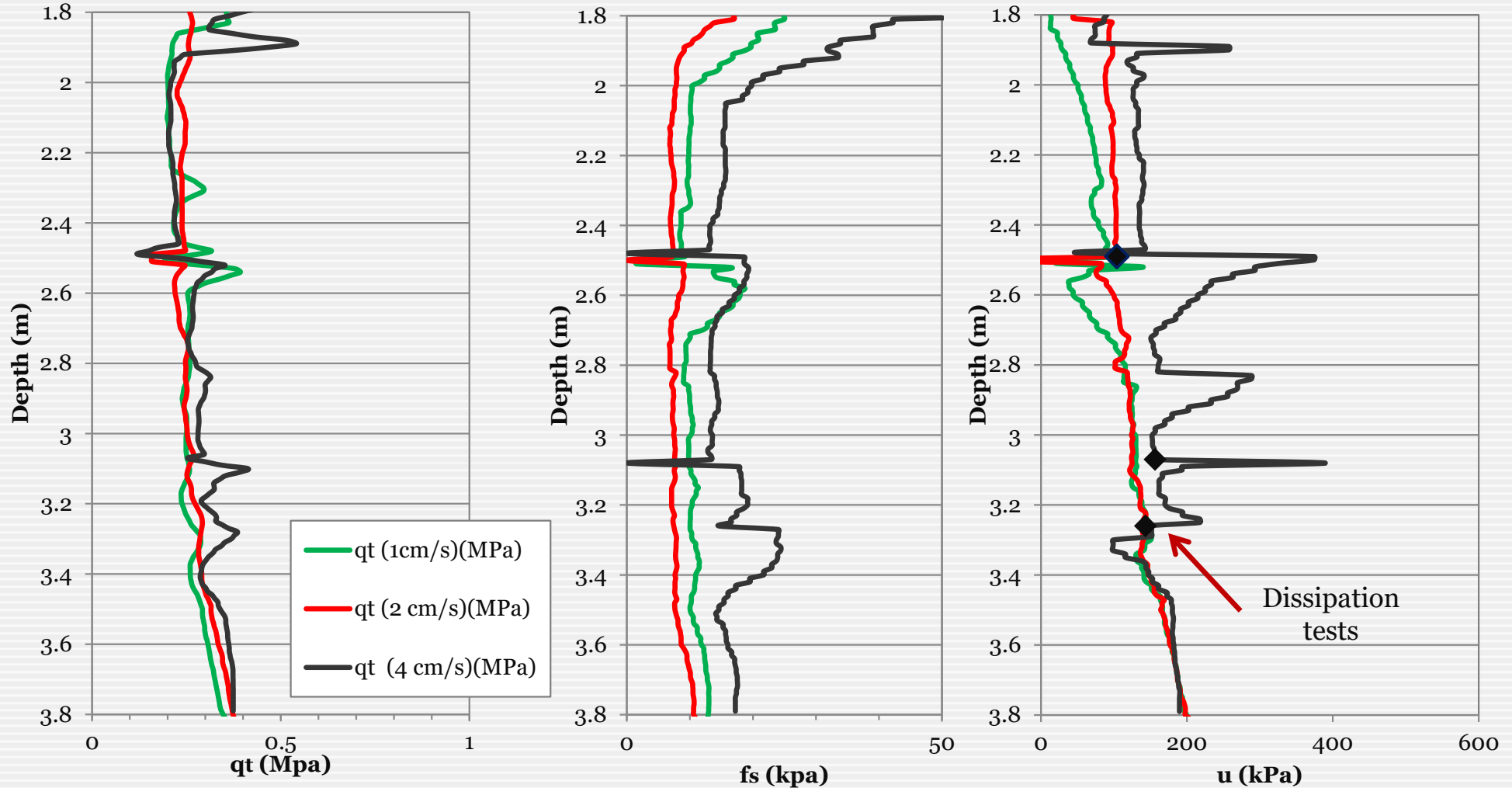
$R = 1.78 \text{ cm}, U = 2 \text{ cm/s}$



# Main goal & activities



# Experimental activities at the Livorno port area: preliminary results

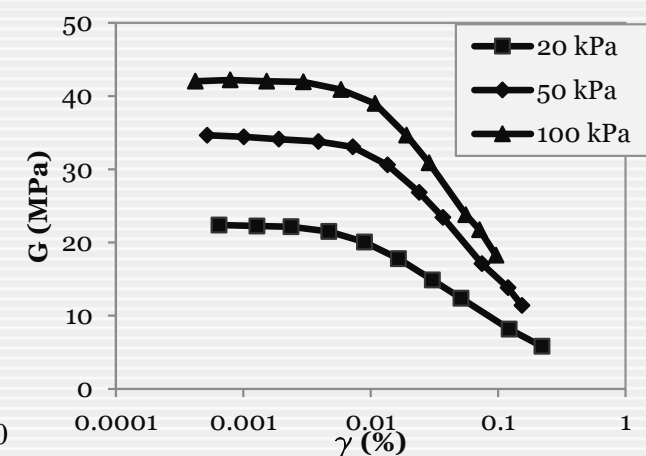
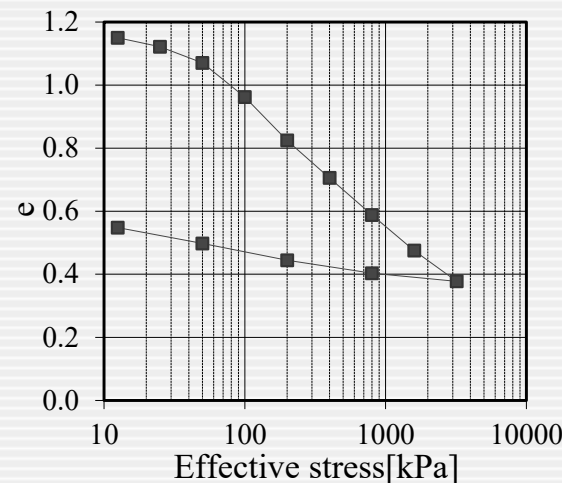
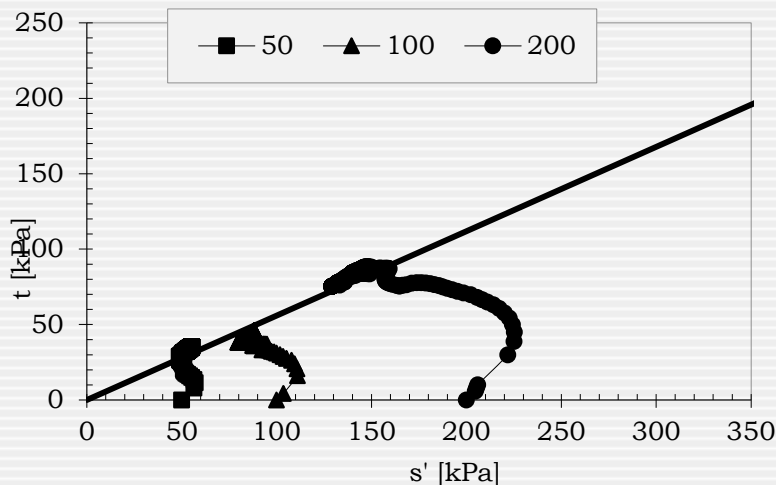


# Experimental activities at the Livorno port area: preliminary results

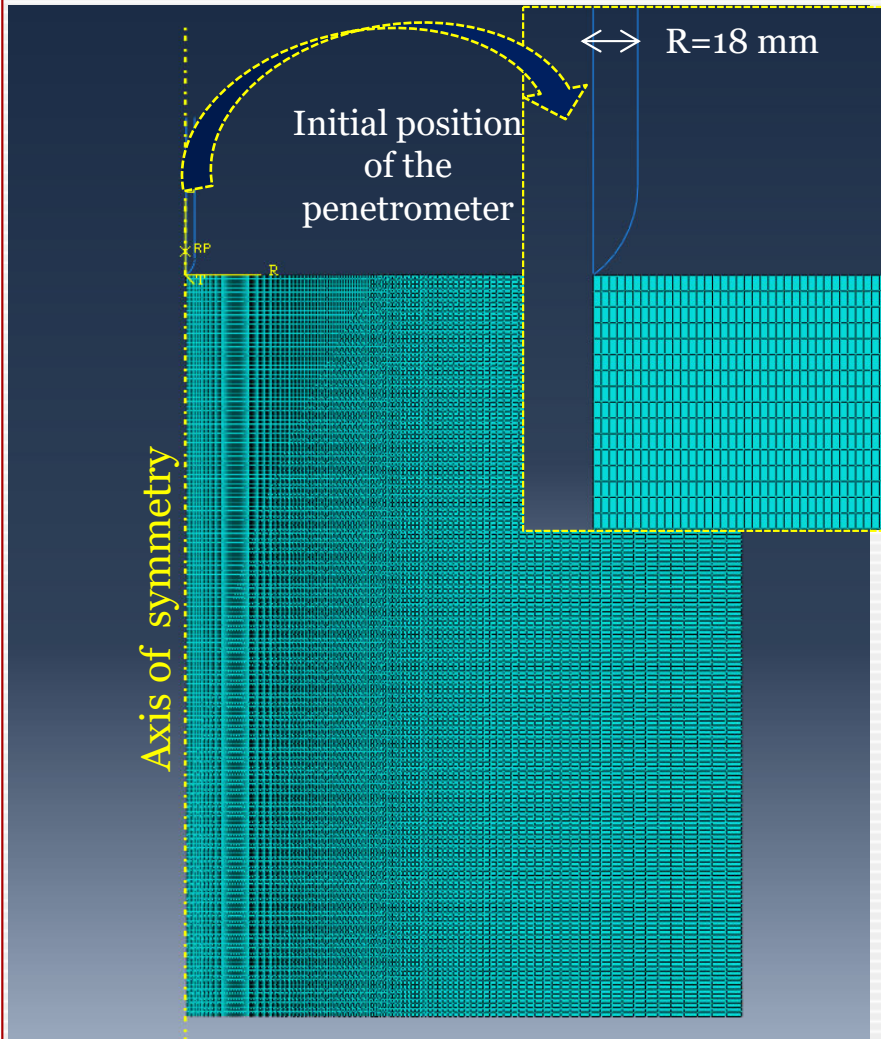


- Incremental loading oedometer test
- Oedometer test with constant rate of strain
- Triaxial test TxCIU (50, 100, 200 kPa)
- Resonant column test (20, 50, 100 kPa)

n° reg.	campione	profondità (m)		Wn (%)	$\gamma$ (kN/m <sup>3</sup> )	e <sub>0</sub>	$\sigma'_p$ (kPa)	$\sigma'_{v0}$ (kPa)	OCR	K (cm/s)	M (MPa)
		da	a								
729	cubico 1	1	1.3	29.1	18.03	0.906	92	23.44	3.93	3.29E-08	1.9
730	cubico 2	1.2	1.5	47.27	16.99	1.306	65	25.49	2.55	2.26E-08	1.4
754	profondo 1	1.6	2.2	44.68	17.54	1.225	43	32.21	1.33	5.86E-08	1.3
755	profondo 2	2	2.5	42.72	17.7	1.174	40	34.93	1.15	4.24E-08	0.9
756	profondo 3	2.5	3	40.01	18.75	0.972	79	42.03	1.88	6.4E-08	1.4

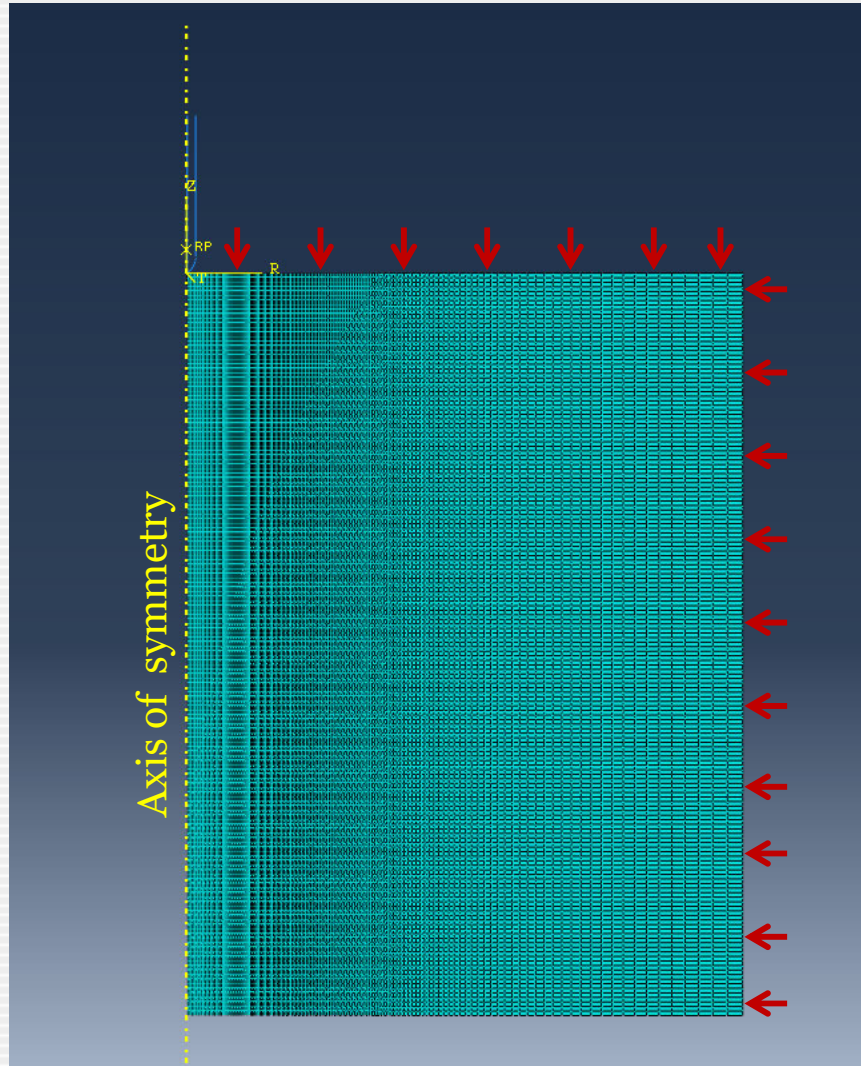


# Finite Elements analyses of cone penetration



- The software used is Abaqus (v. 6.13-2)
- Model A: Undrained penetration process; total stress analysis; Abaqus/Explicit - explicit direct-integration procedure; Arbitrary Lagrangian-Eulerian (ALE) scheme
- Model B: effective stress analysis; Abaqus/Standard - implicit integration procedure; Updated Lagrangian scheme (UL)
- The cone penetrometer is treated as a rigid body (2D analytical surface); contact interaction is assumed frictionless; rate of 2 cm/s

# Finite Elements analyses of cone penetration



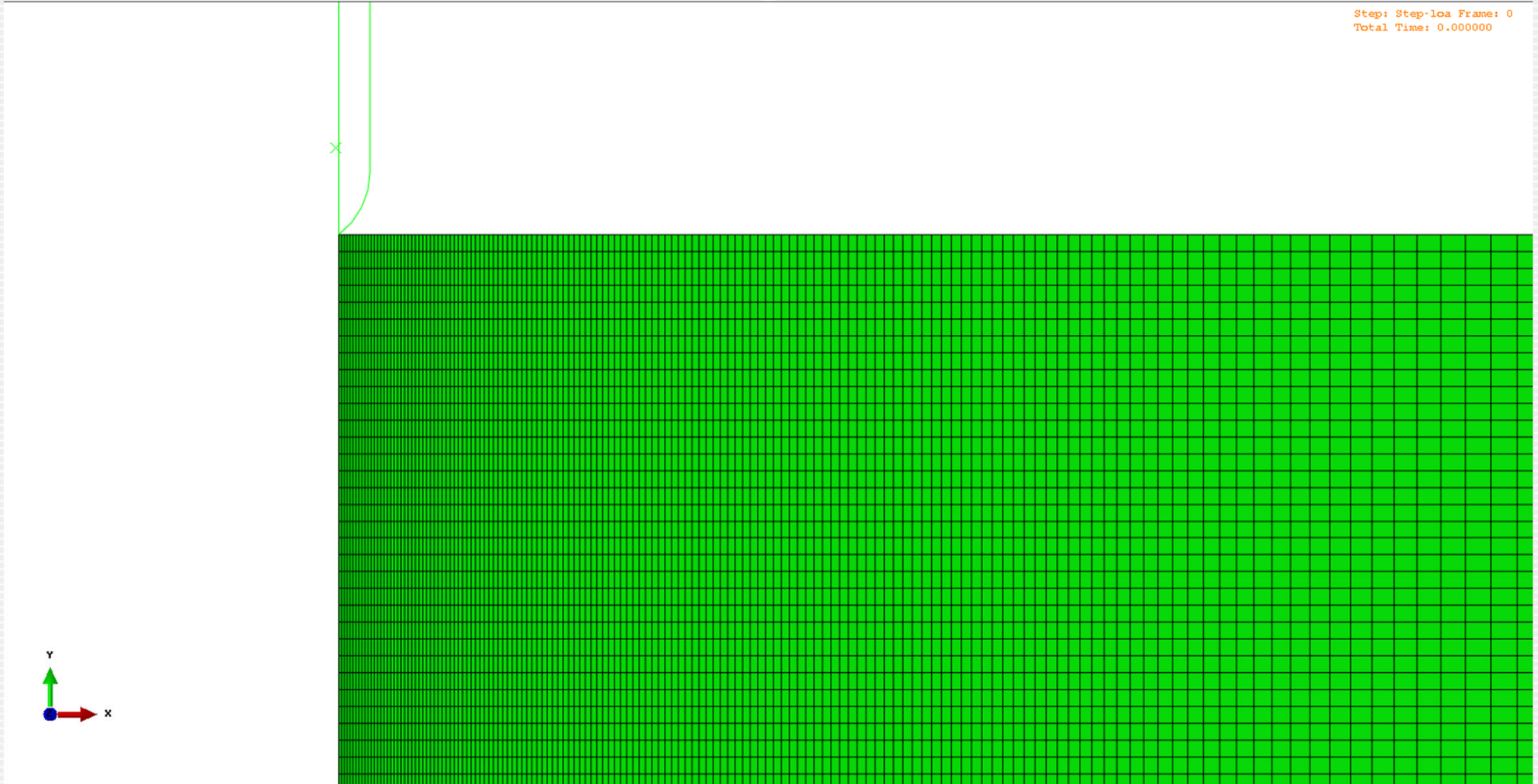
Model A - Tresca	
Model geometry	1.2 m x 1.6 m
Penetrometer	R = 18 mm
Poisson's ratio	0.49
G	960 kPa
Su	20 kPa
Initial vertical and horizontal load	35 kPa
Adaptive technique	ALE method
Abaqus/Explicit	



# ALE method – Abaqus/Explicit



Step: Step-1oa Frame: 0  
Total Time: 0.000000

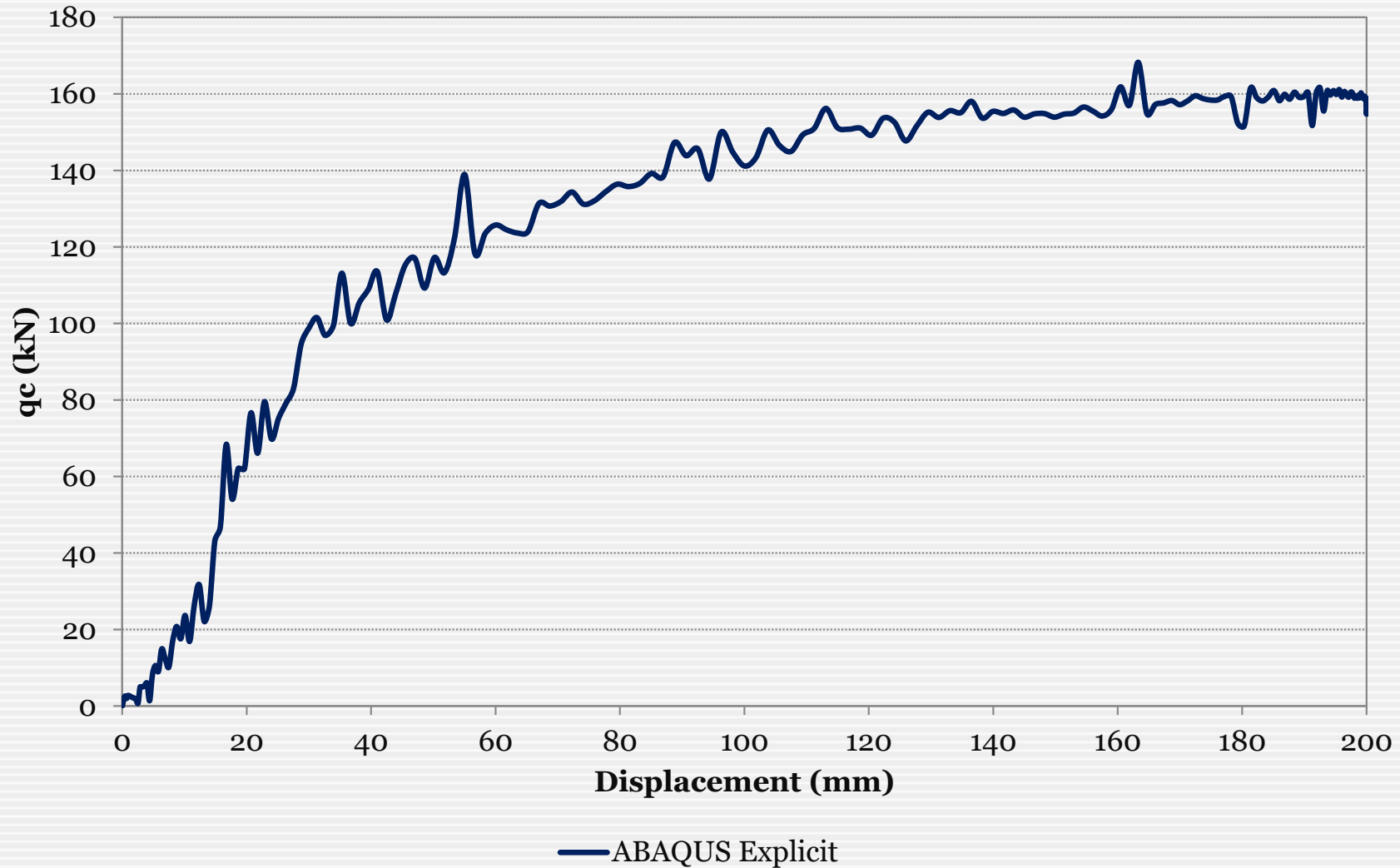


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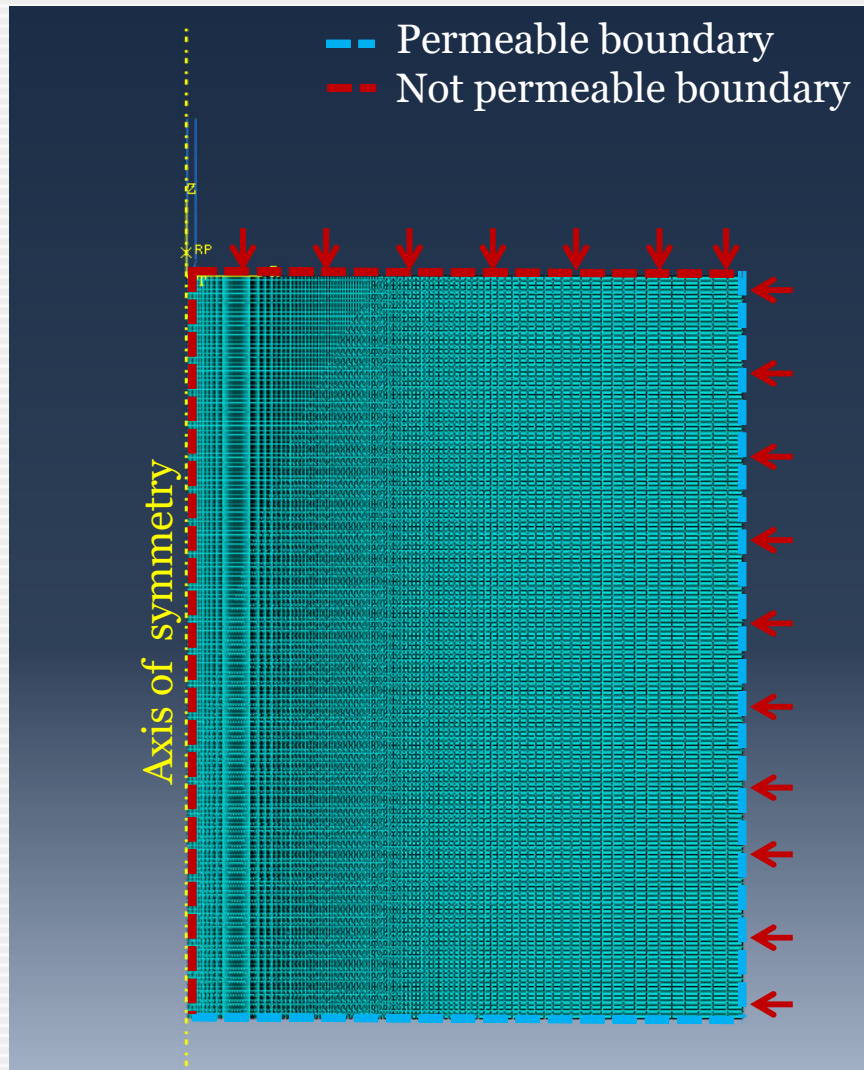
# ALE method – Abaqus/Explicit



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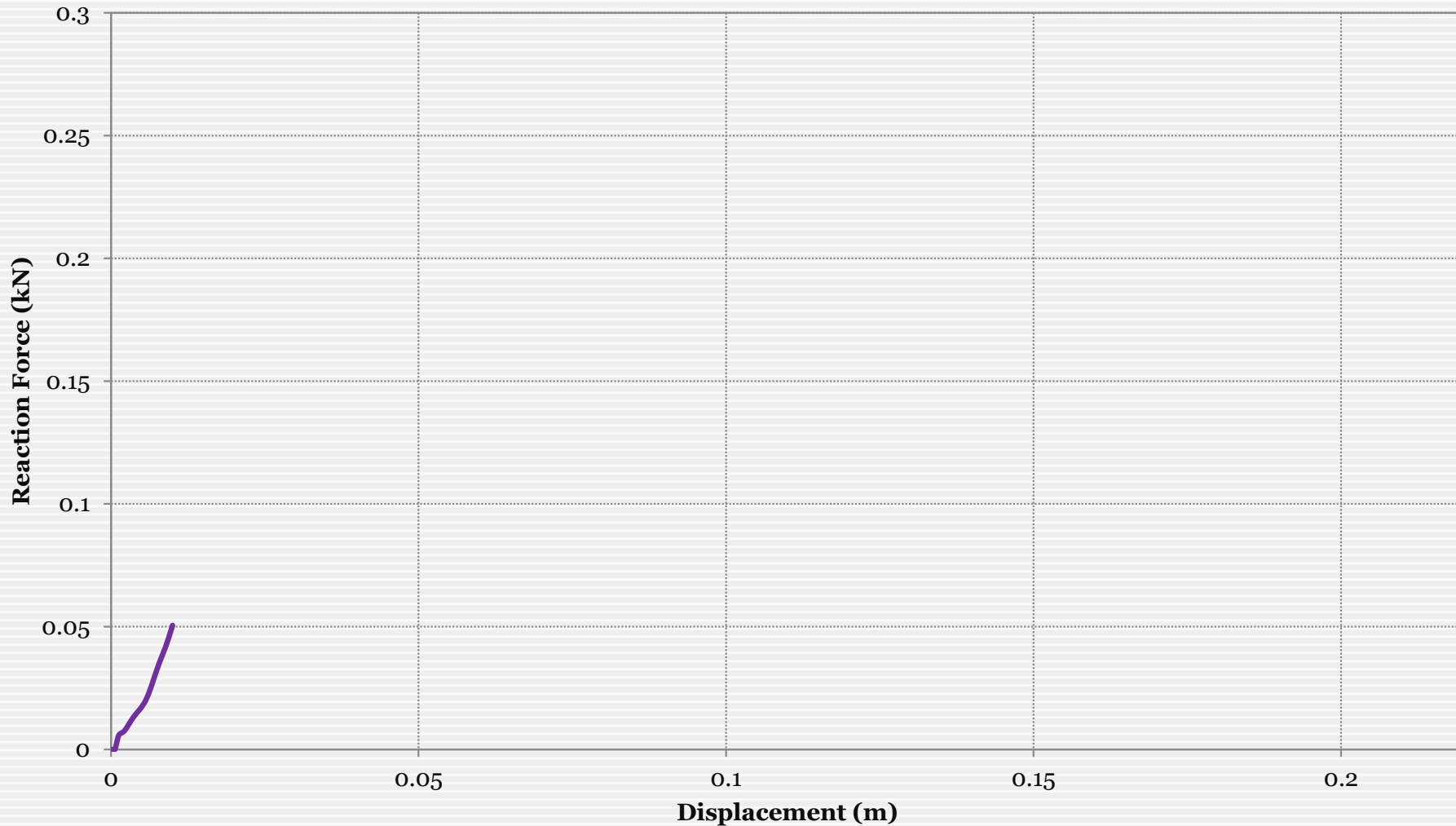
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# Finite Elements analyses of cone penetration



Mohr-Coulomb model	
Model geometry	1.2 m x 1.6 m
Penetrometer	R = 18 mm
Young modulus	2400 kPa
Poisson's ratio	0.25
G	960 kPa
$\varphi$	30°
c'	0 kPa
Initial vertical and horizontal load	35 kPa
Initial pore water pressure	0 kPa
Initial void ratio	1.25
Hydraulic conductivity	k = 1 exp -9 m/s k = 1 exp -6 m/s
Adaptive technique	Updated Lagrangian
Abaqus/Standard	

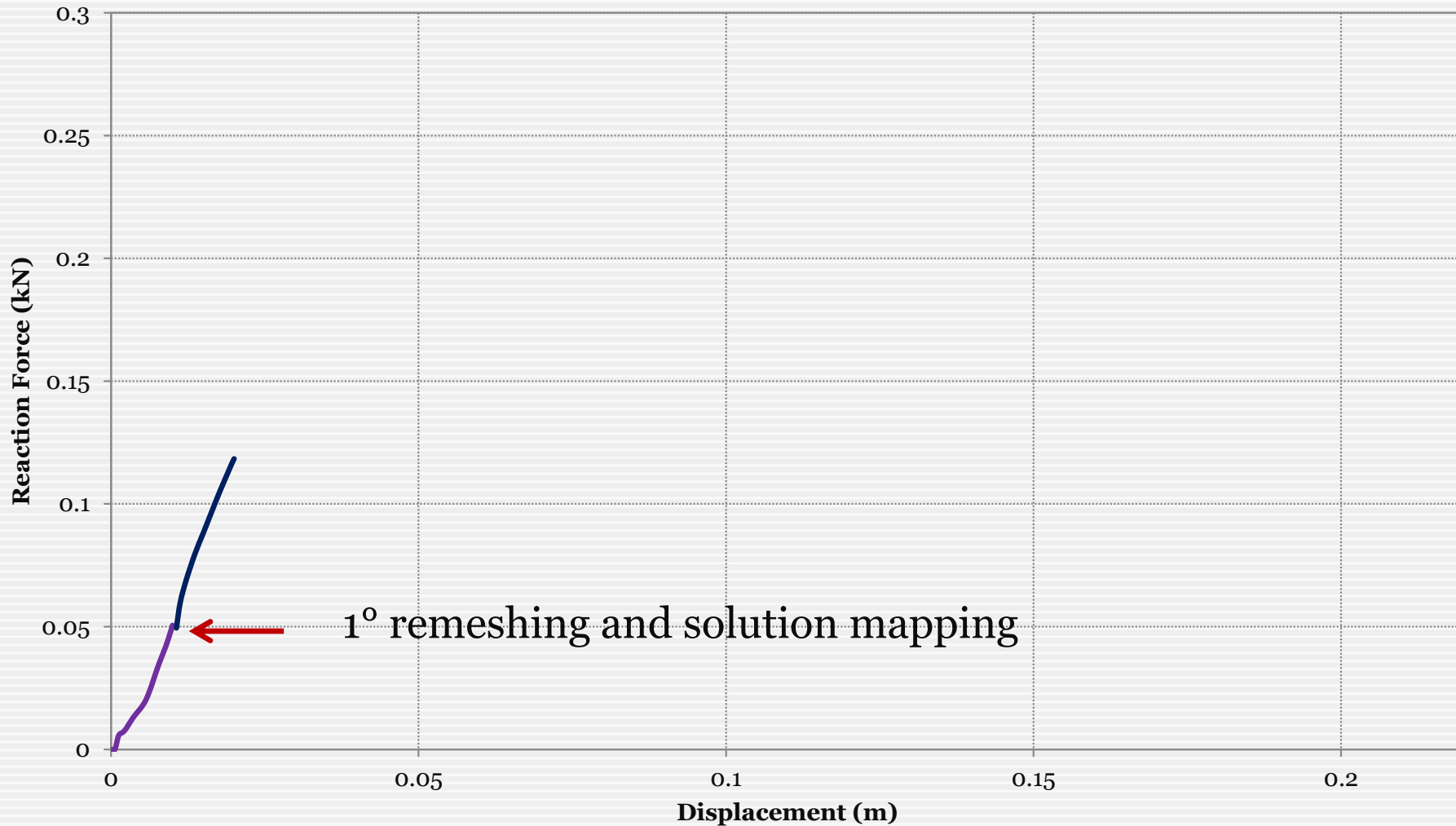
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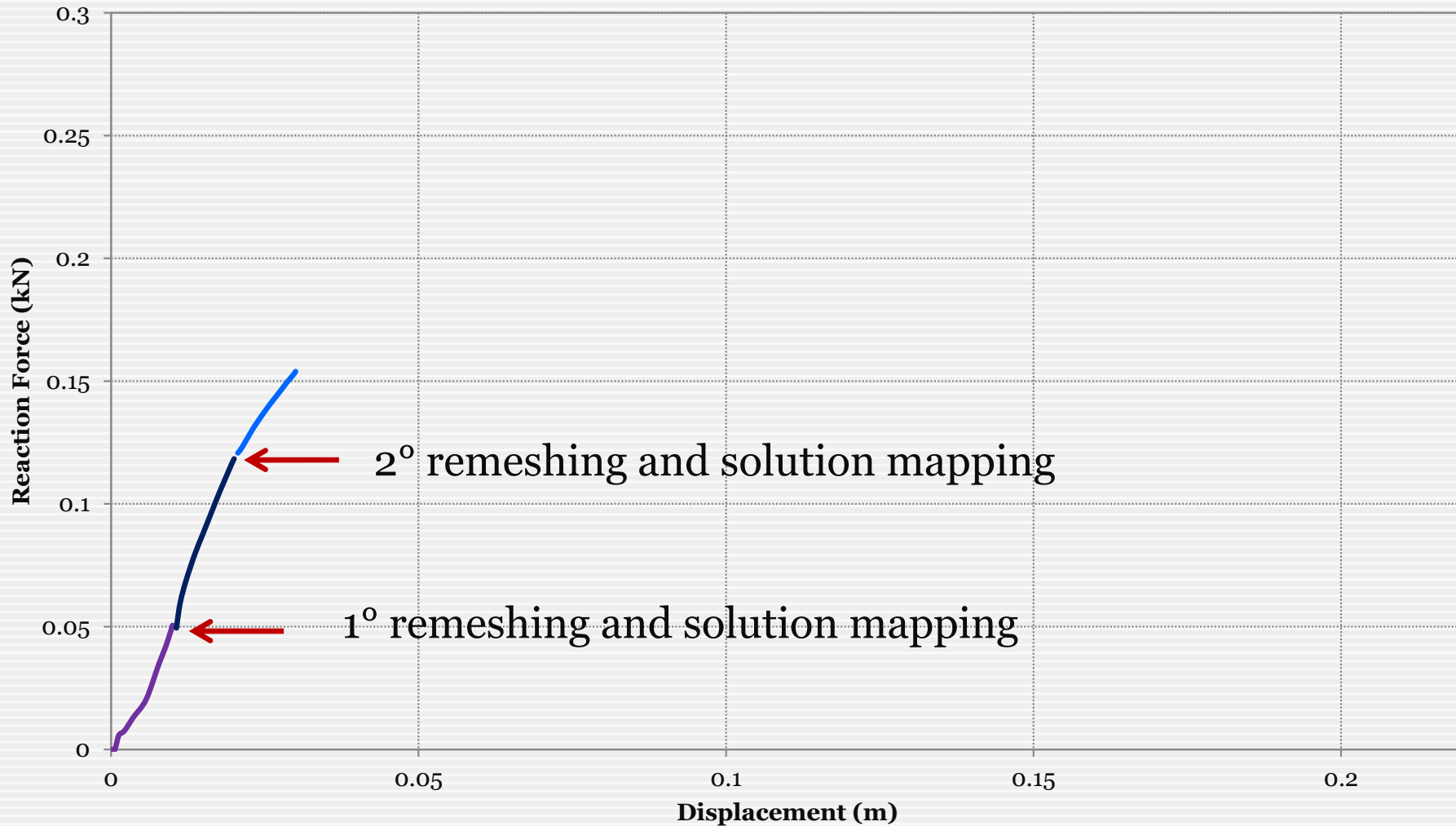
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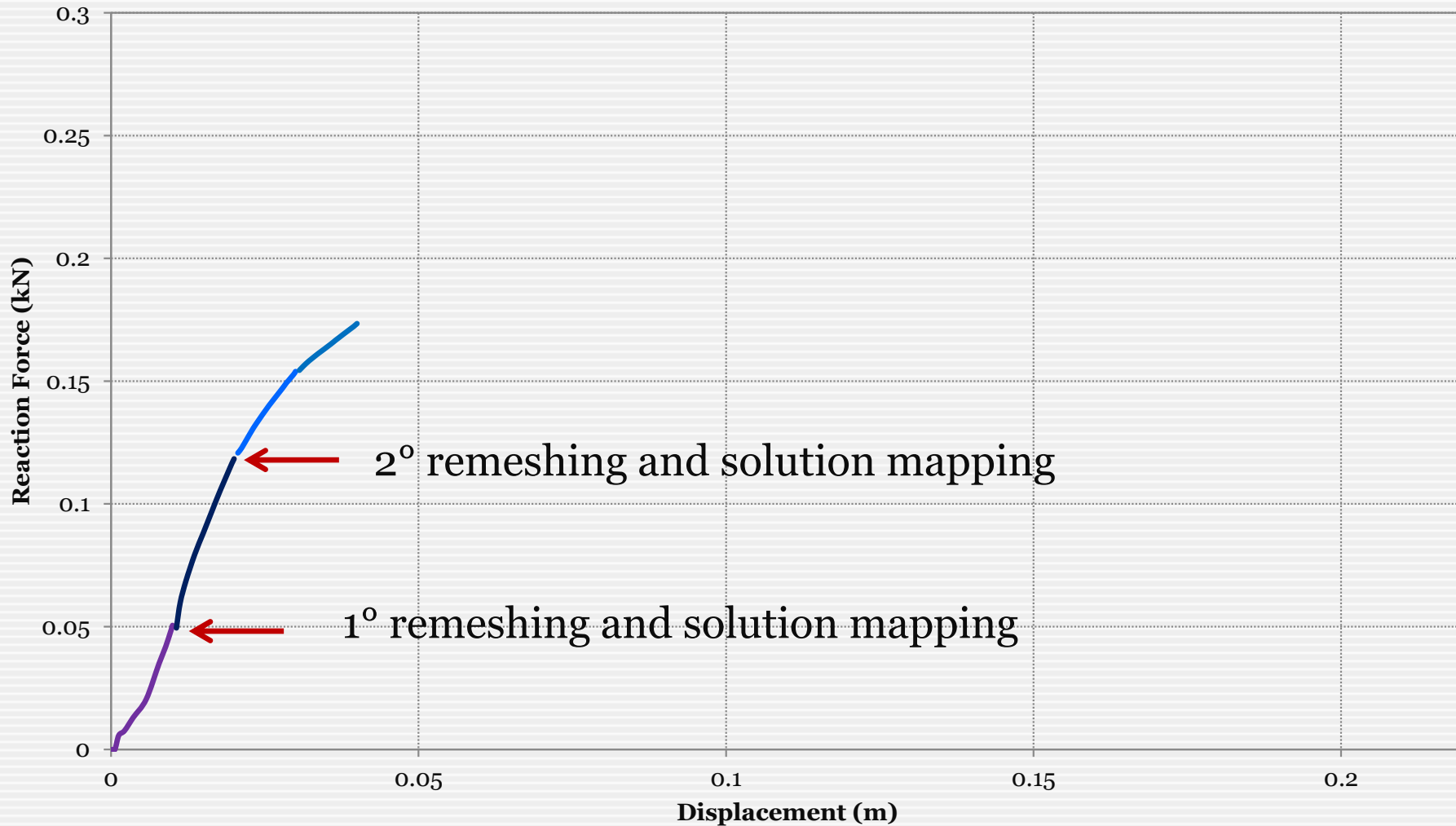
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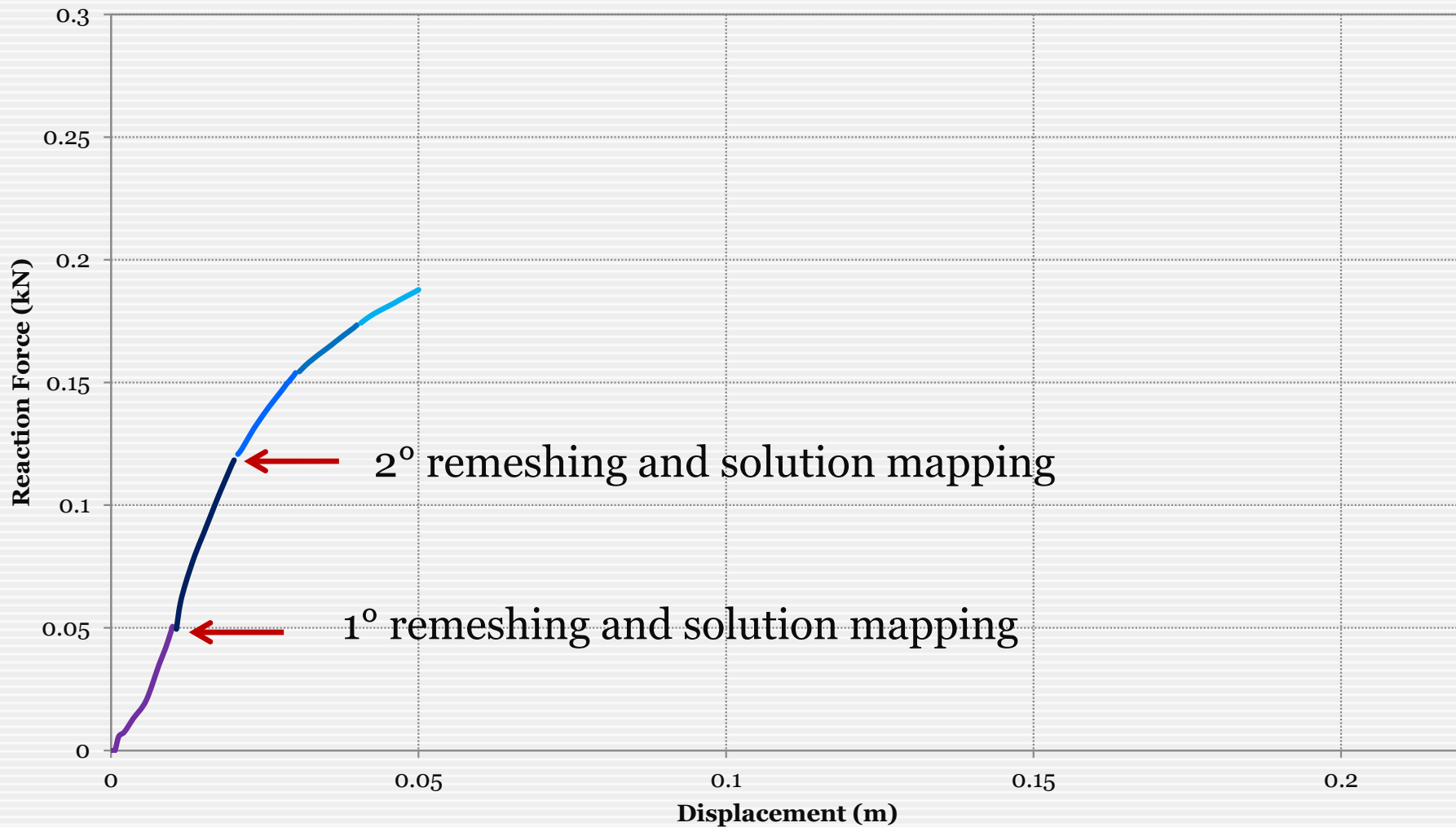
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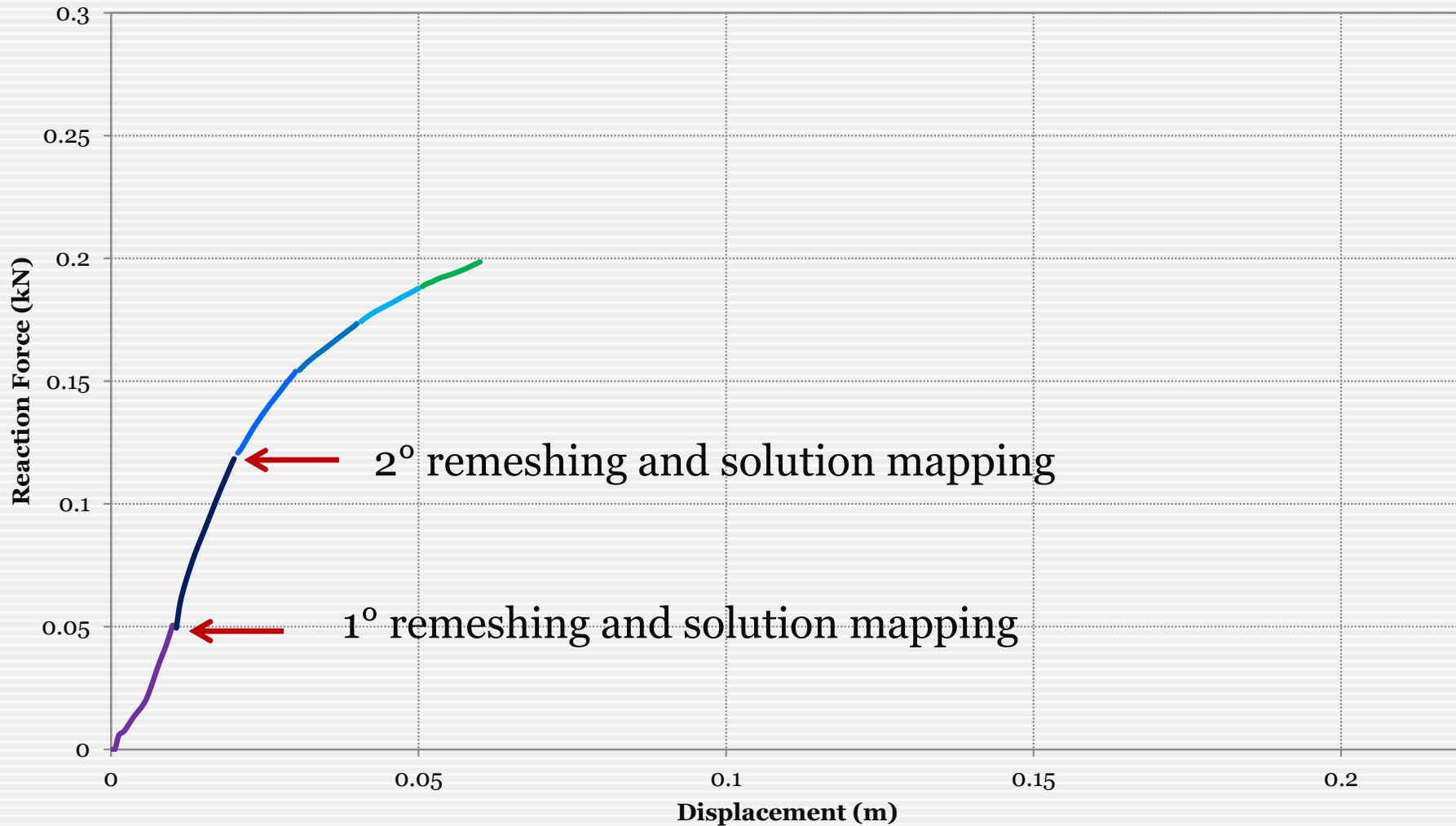
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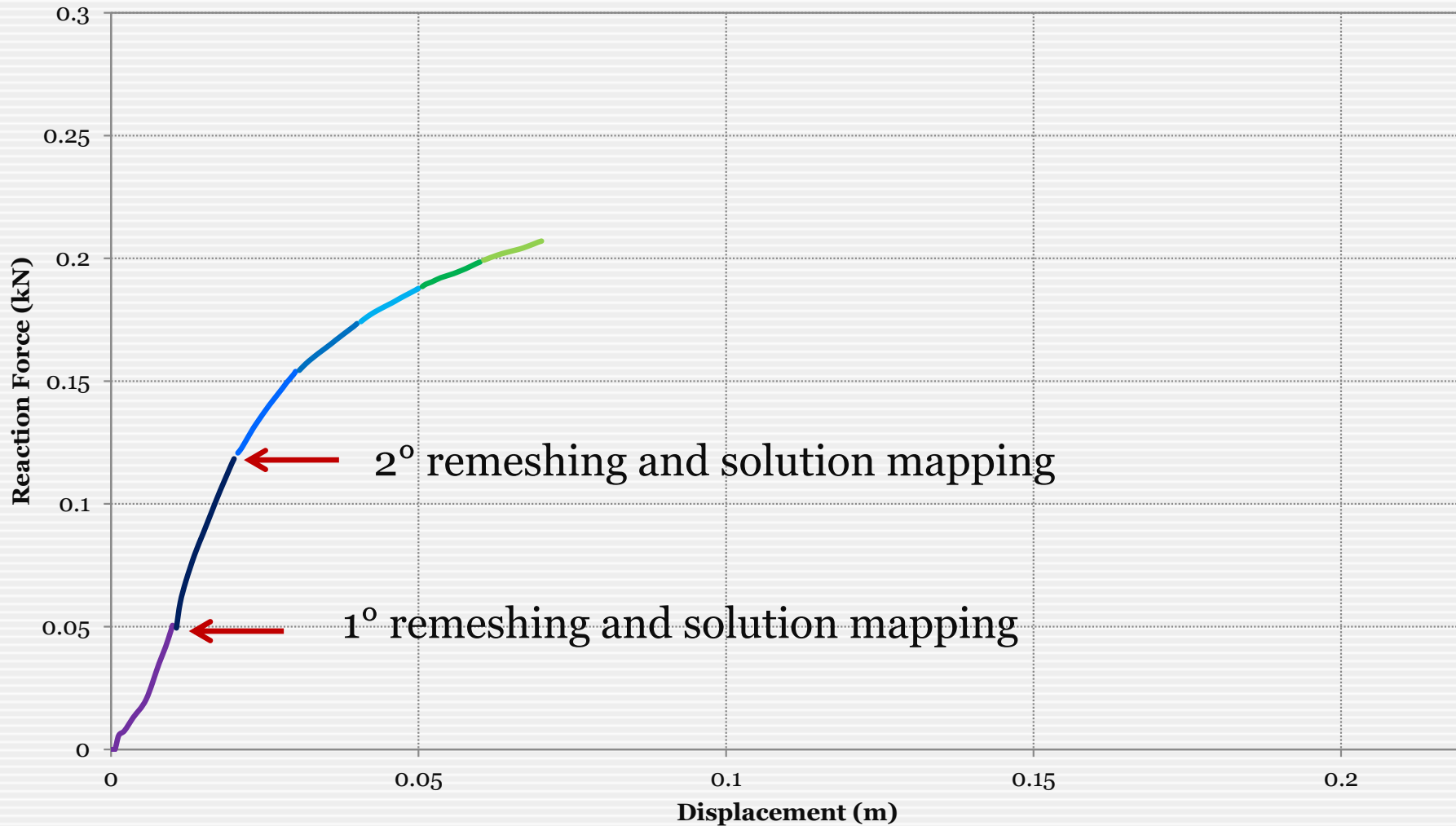


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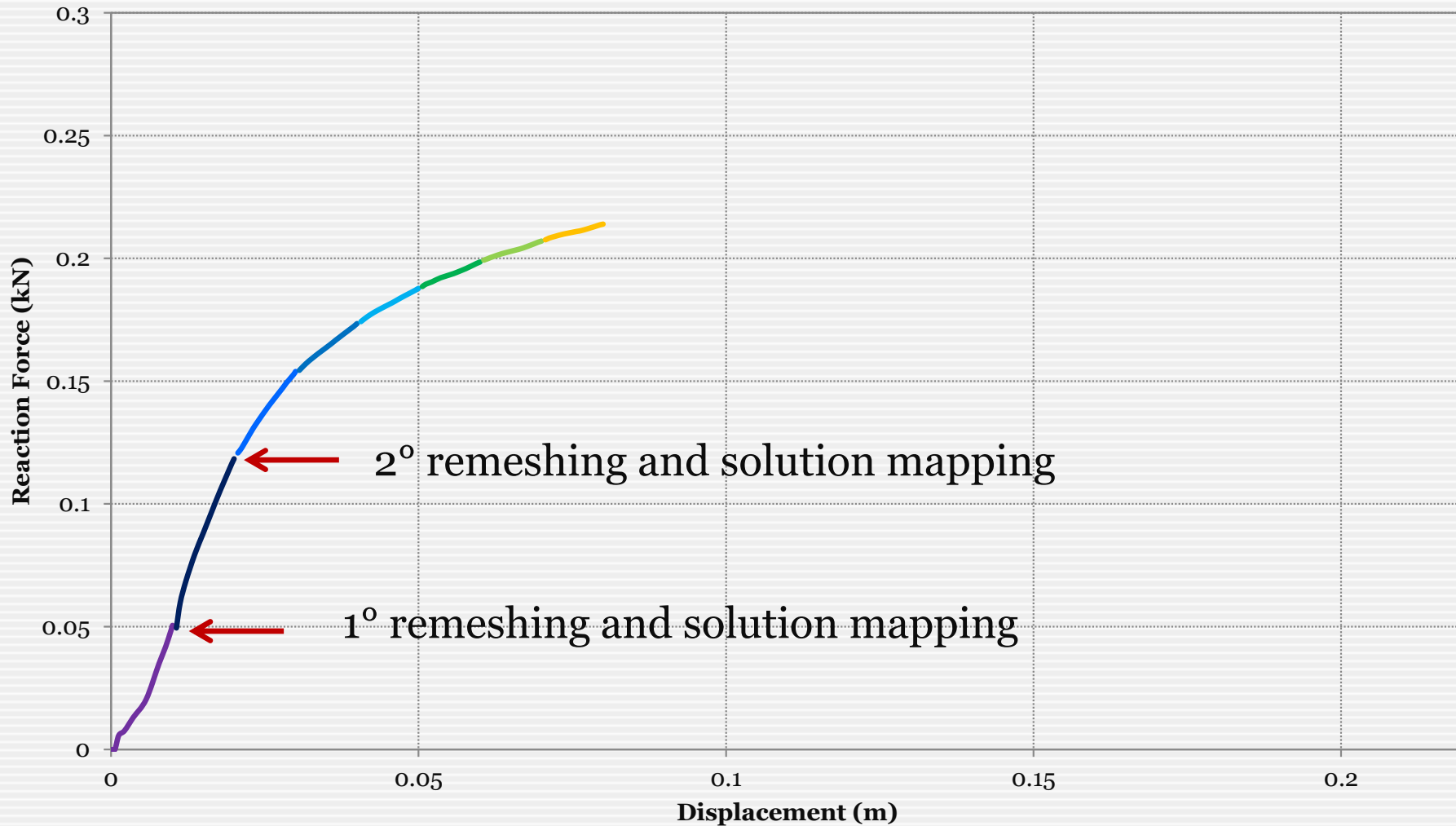
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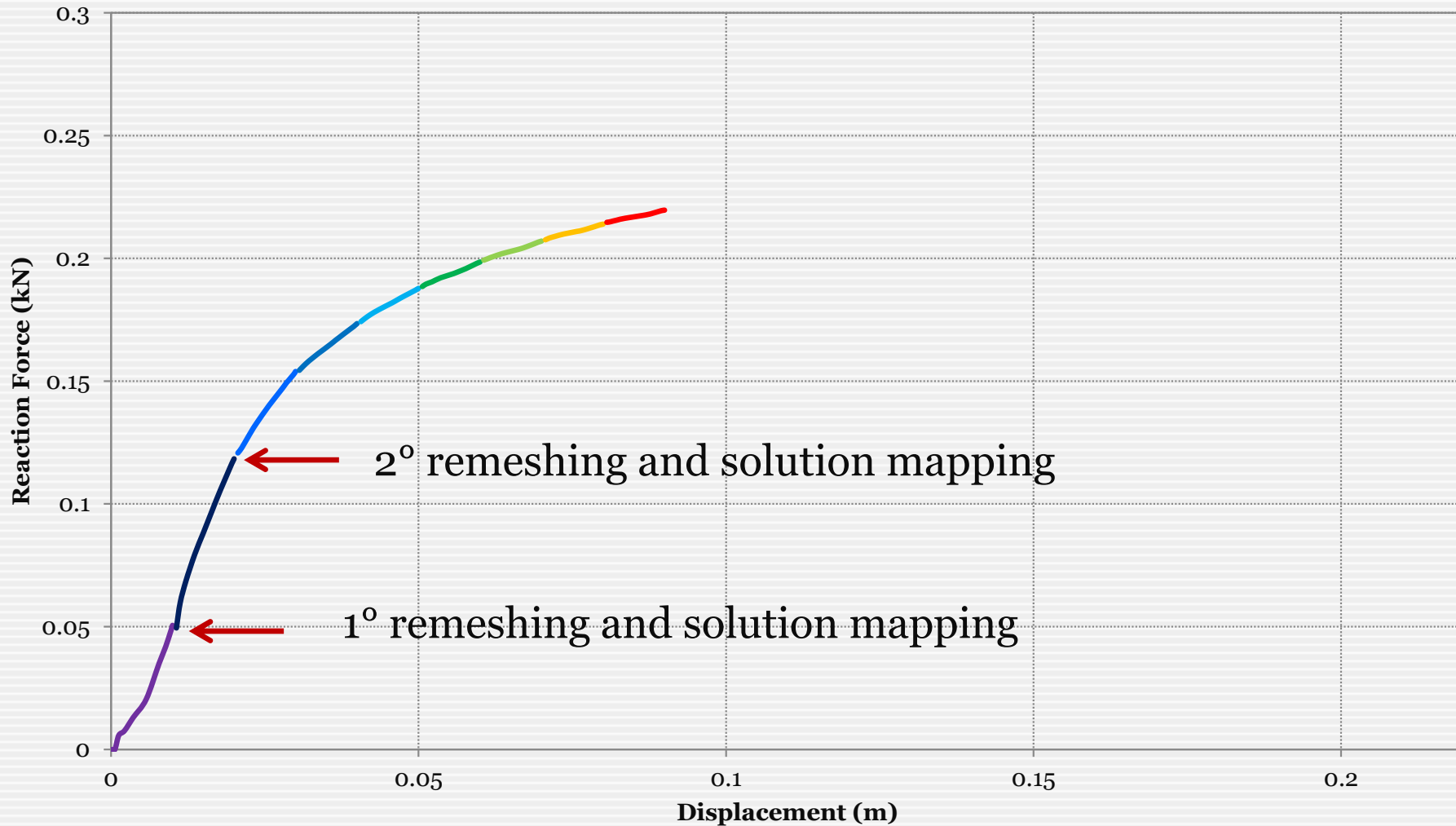
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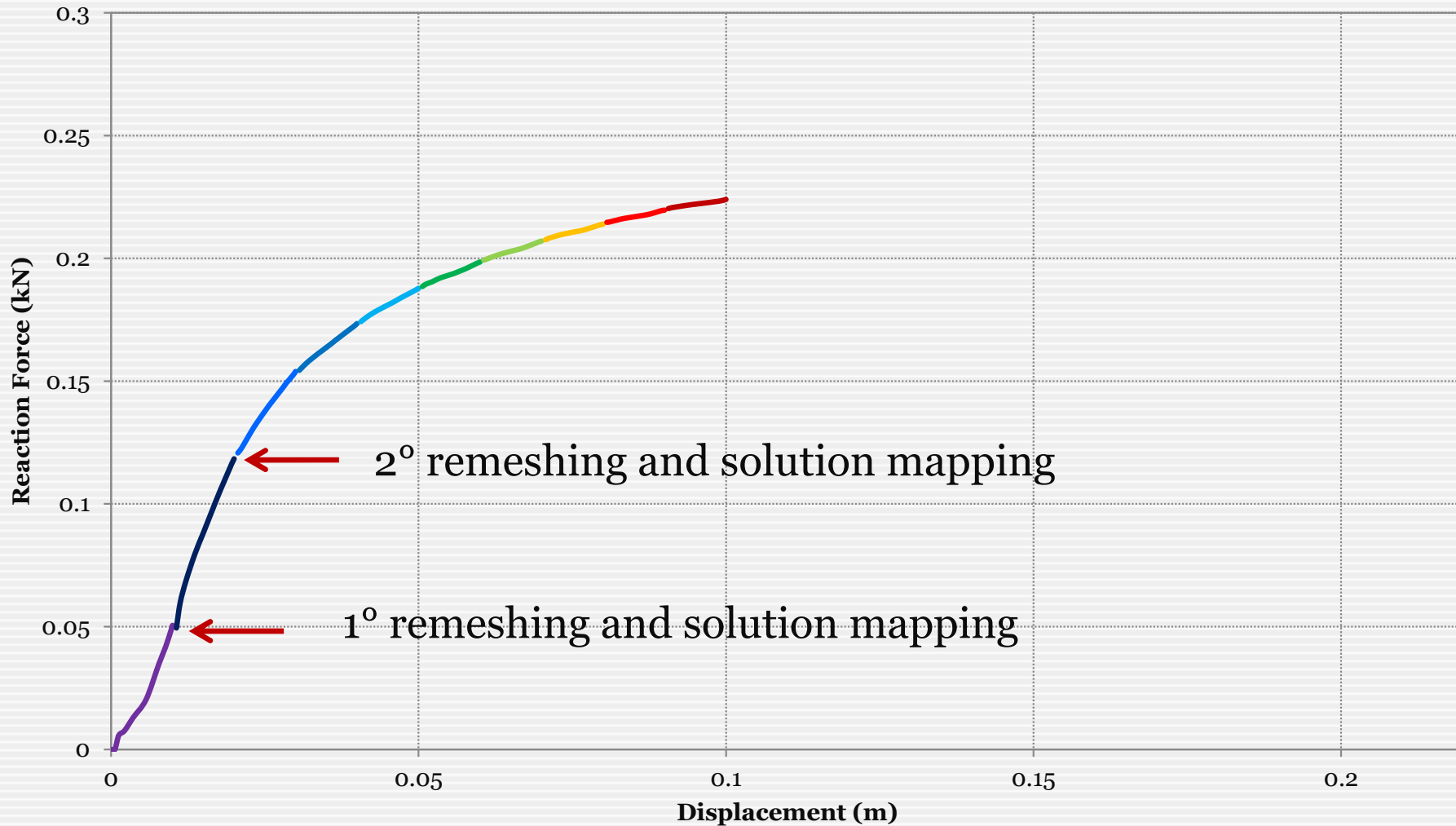
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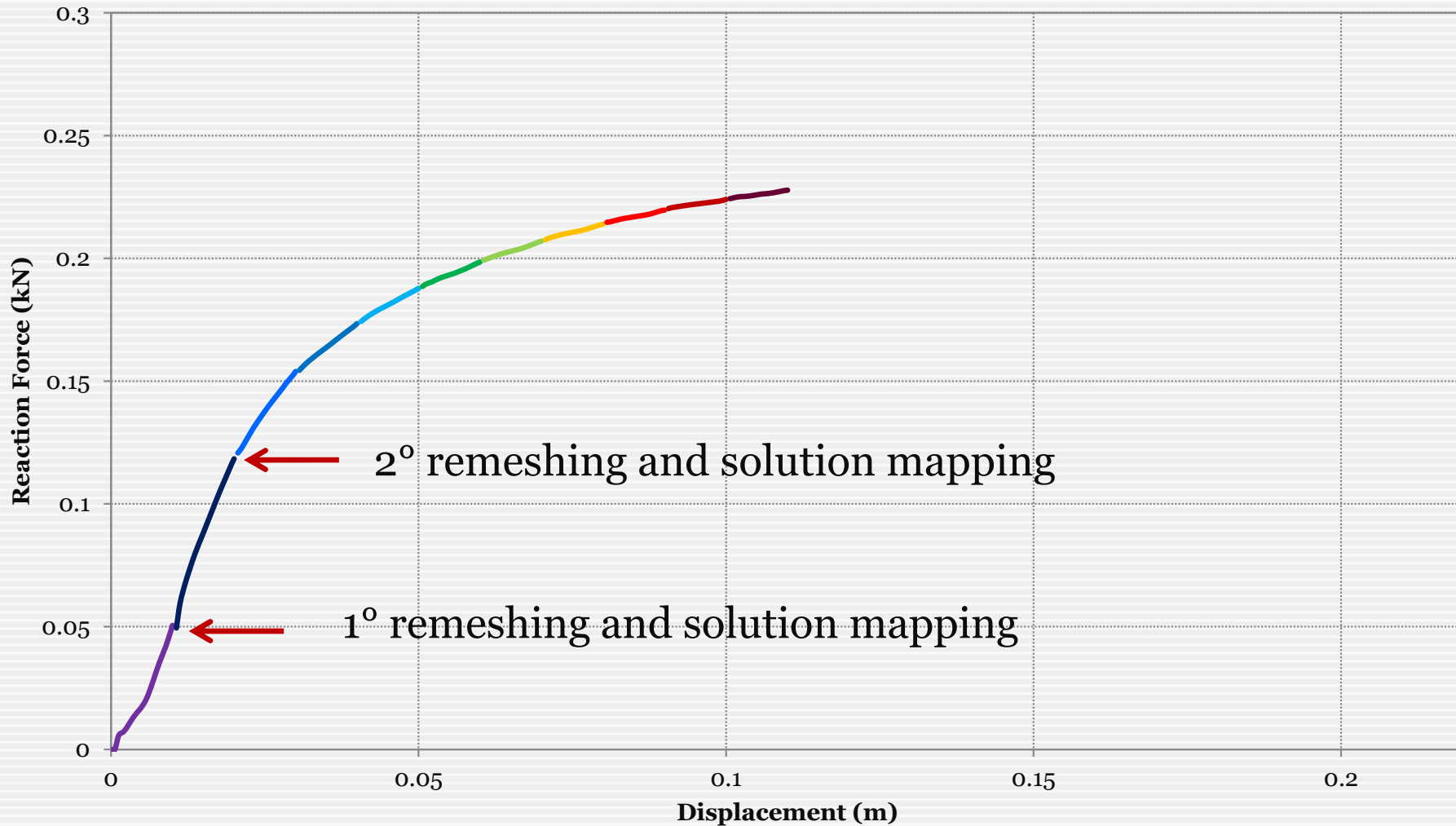
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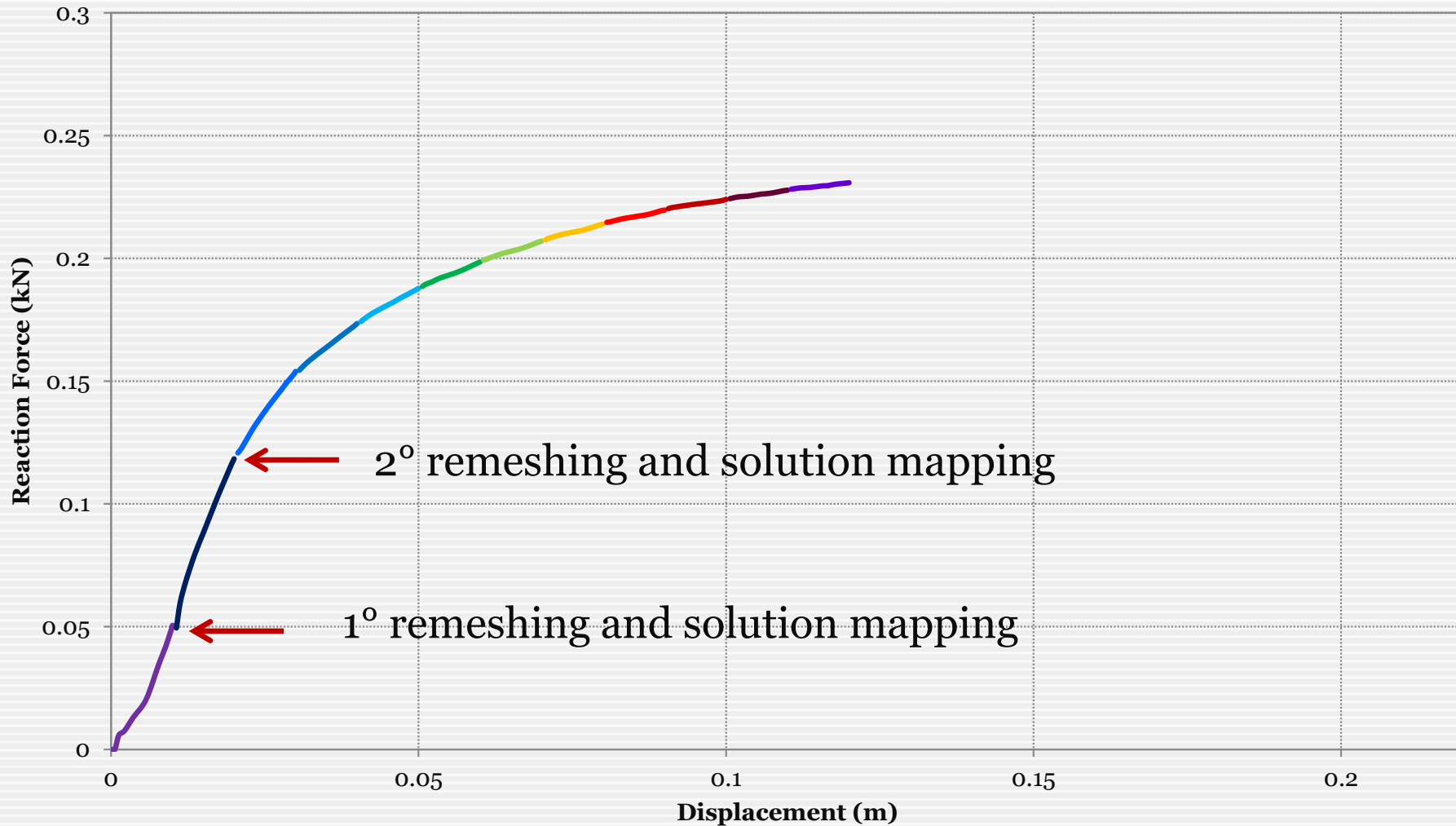
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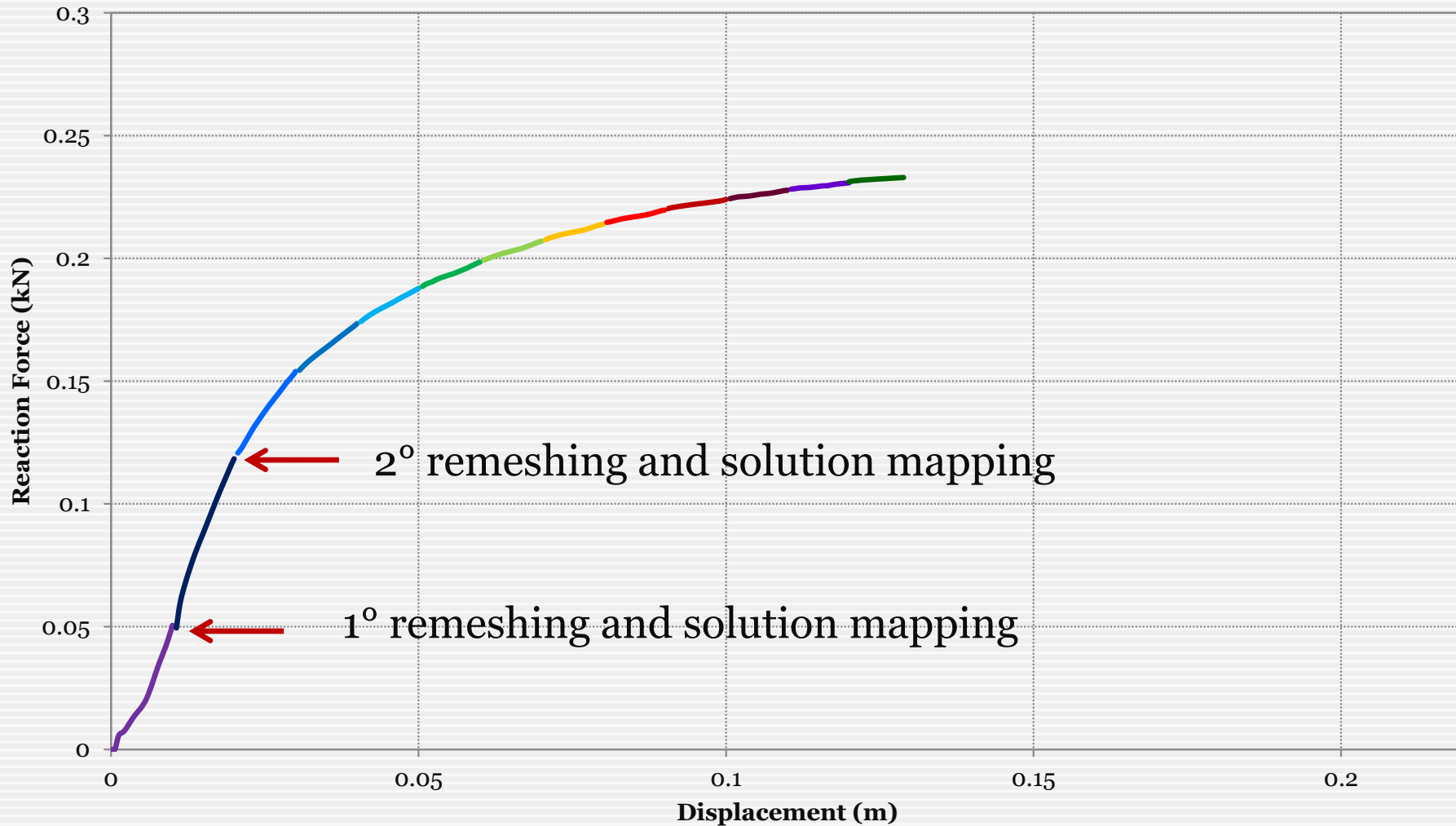
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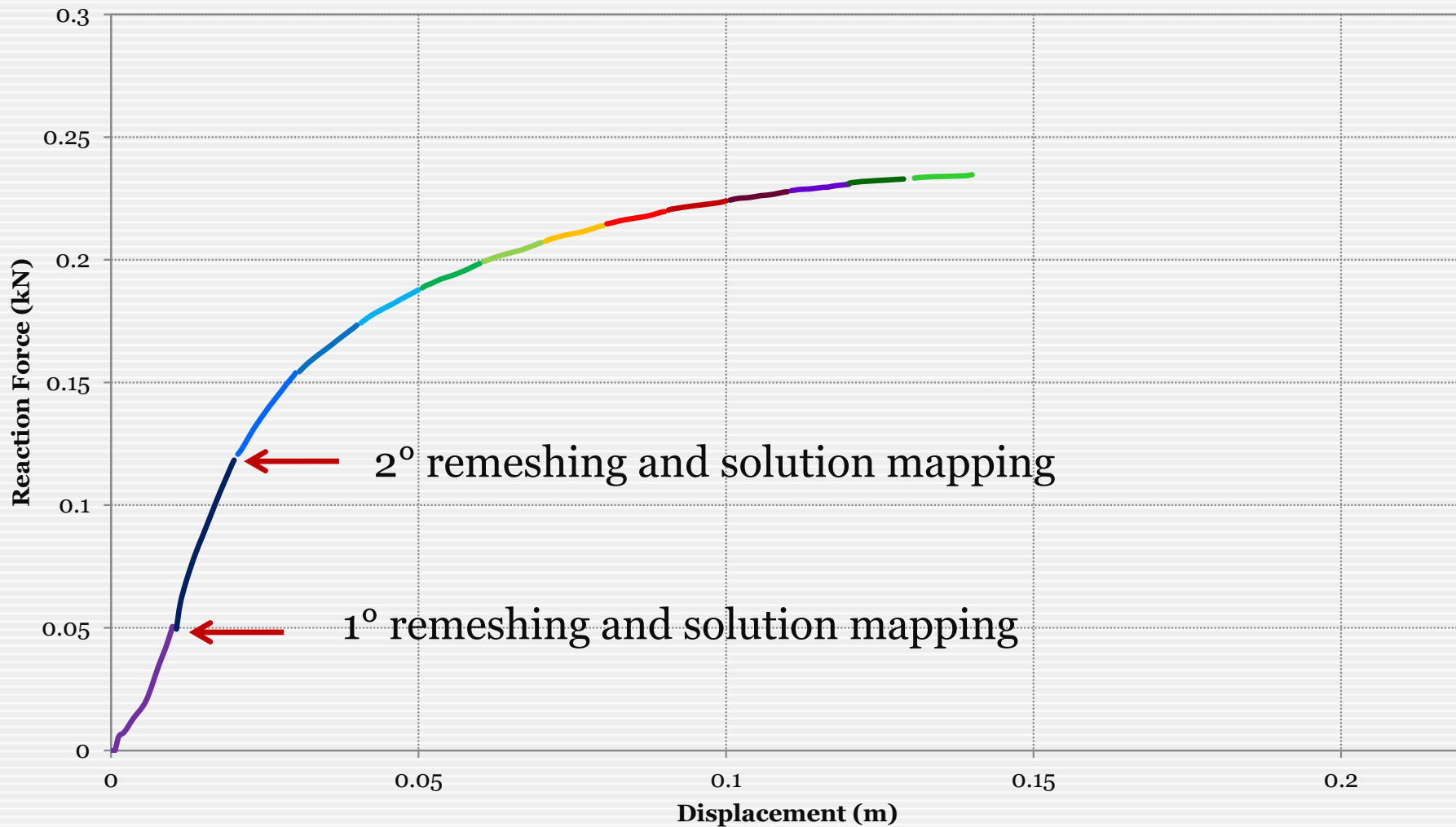
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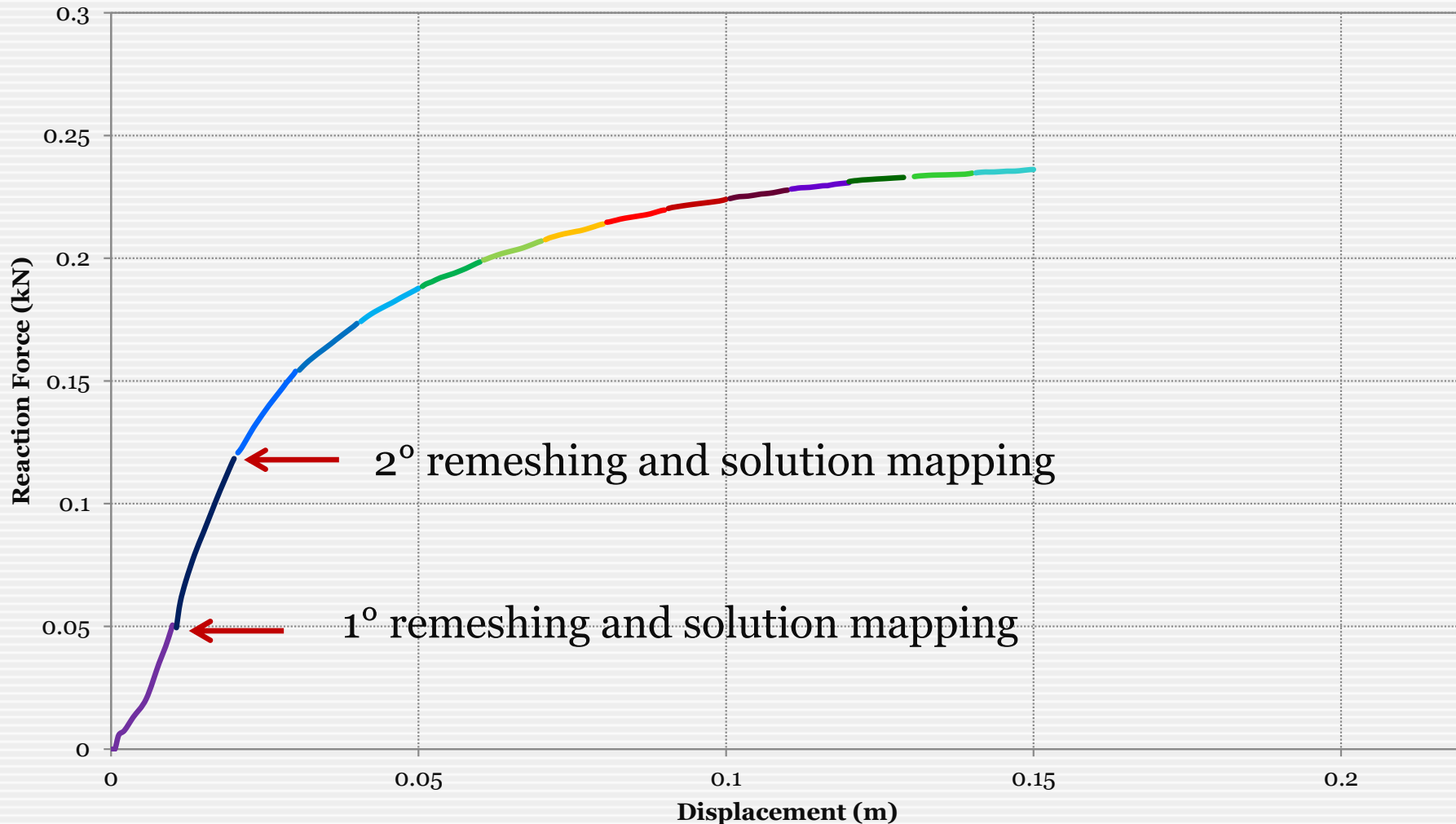


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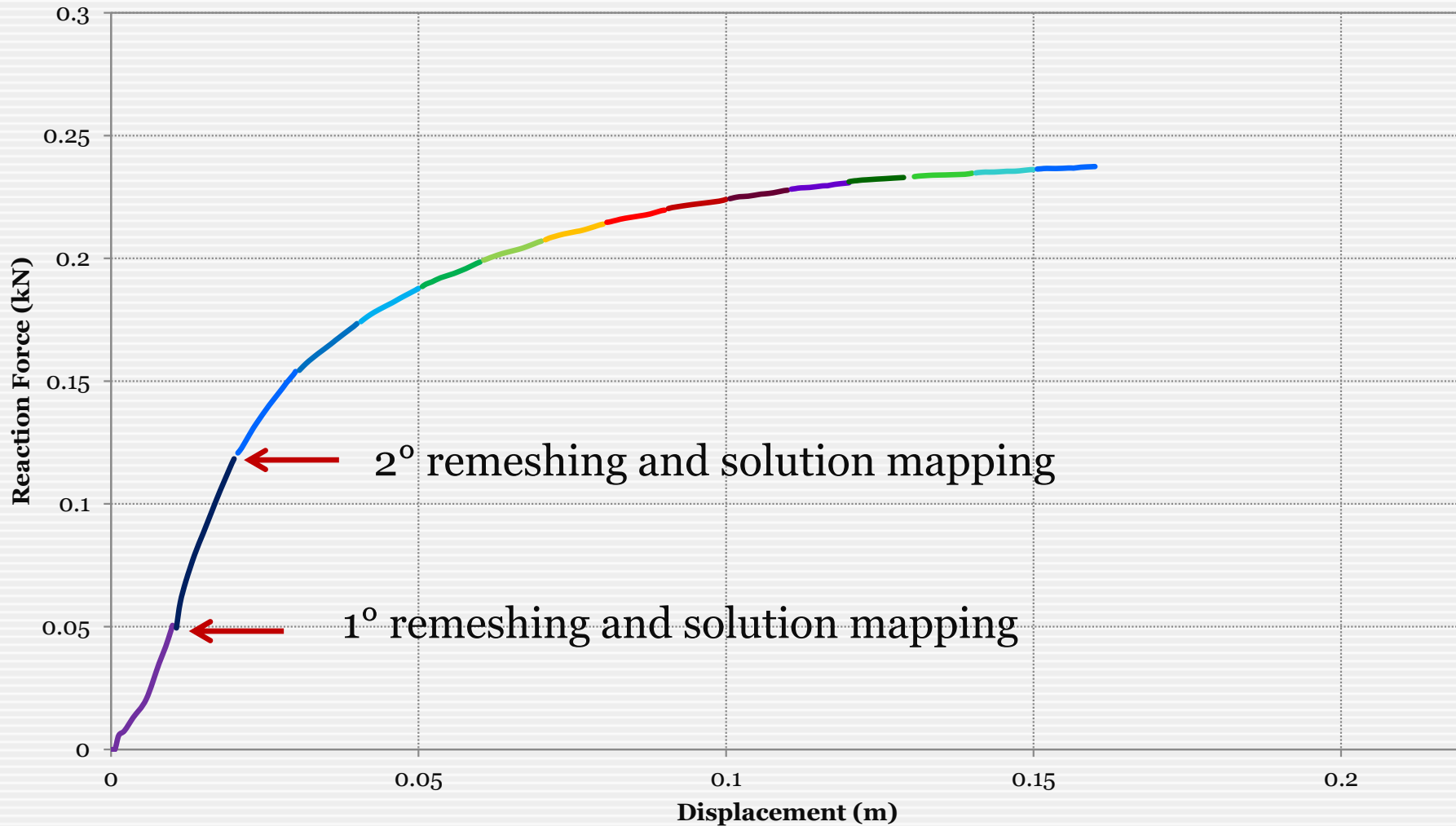
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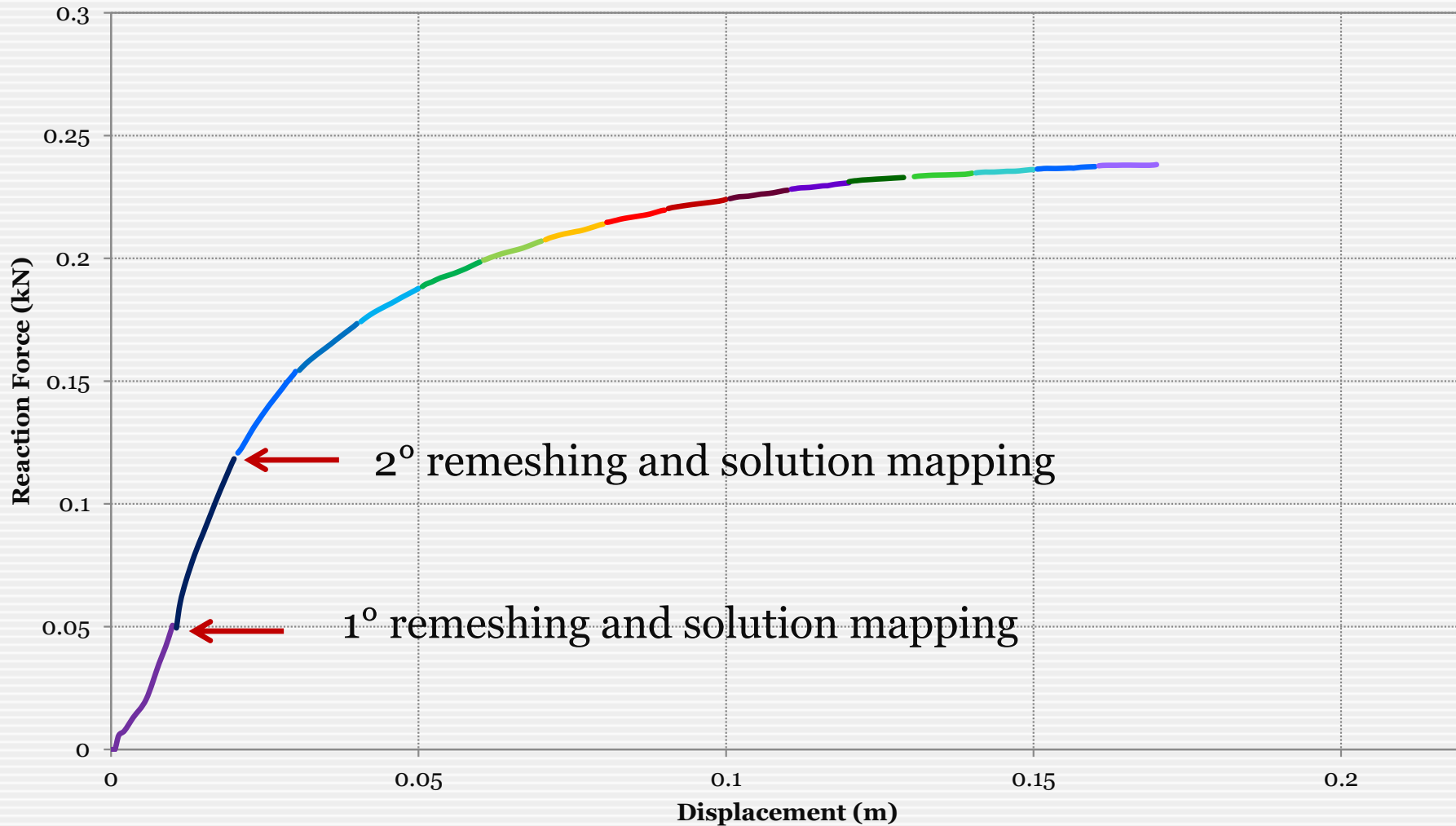
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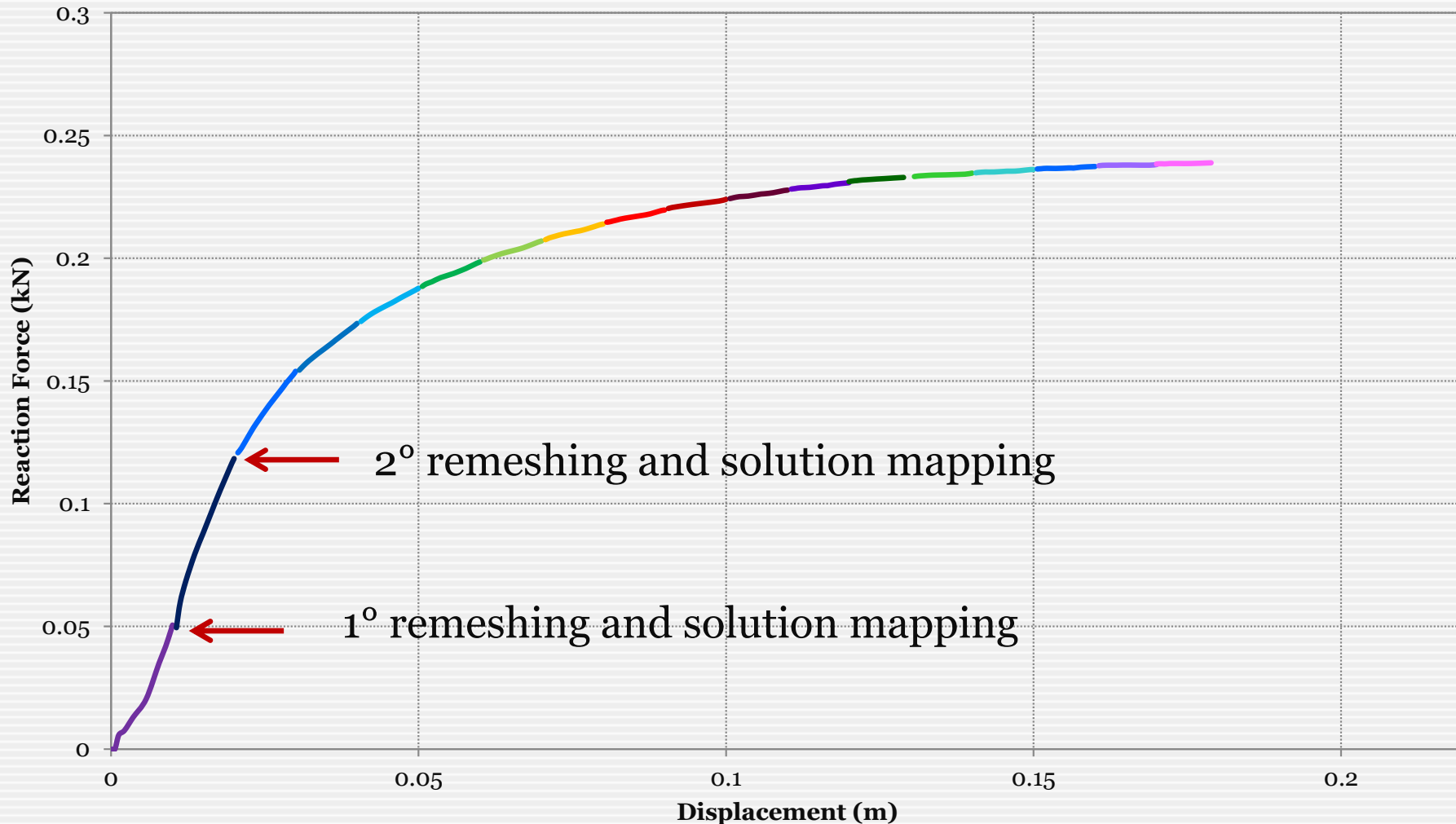
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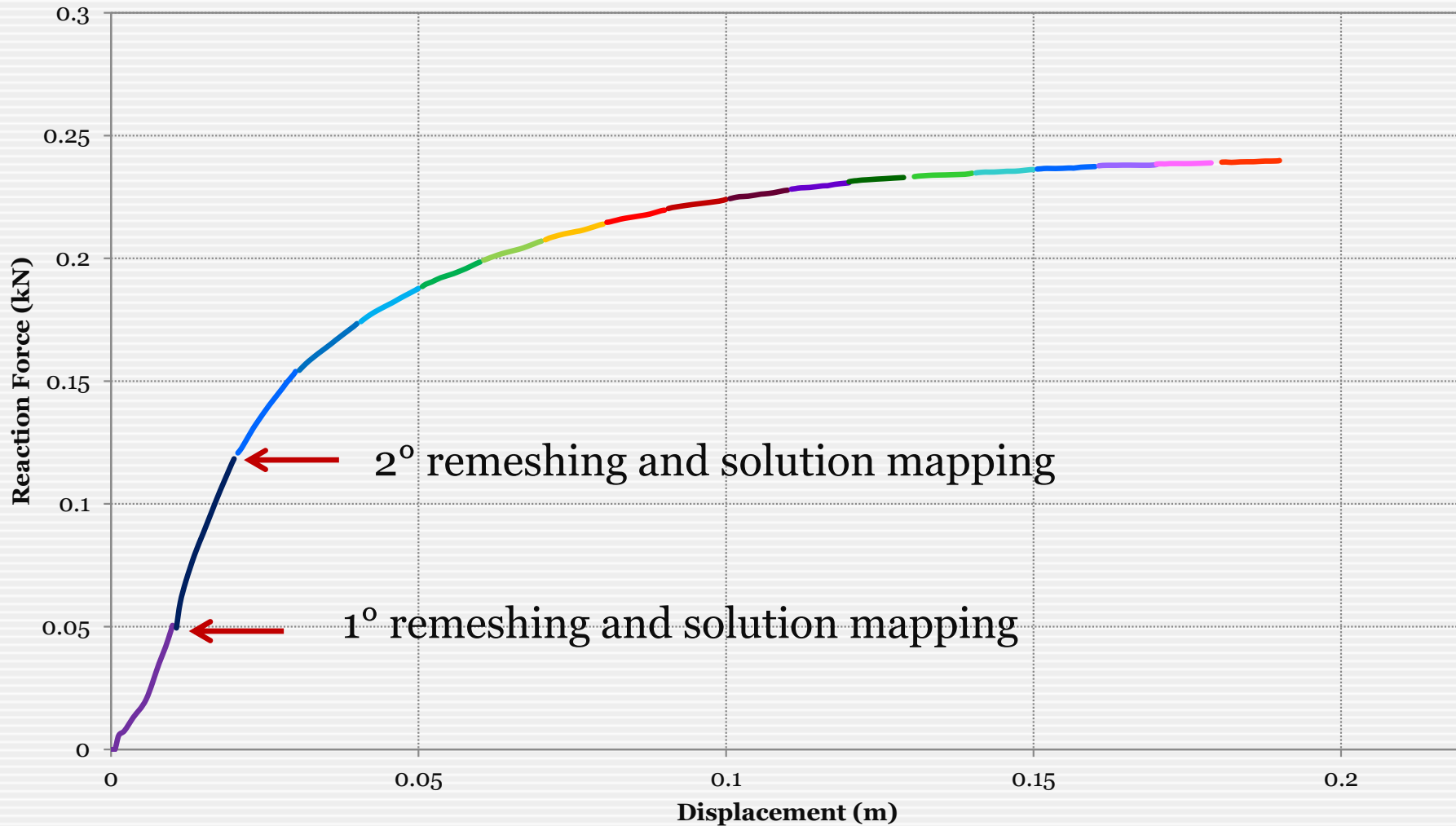
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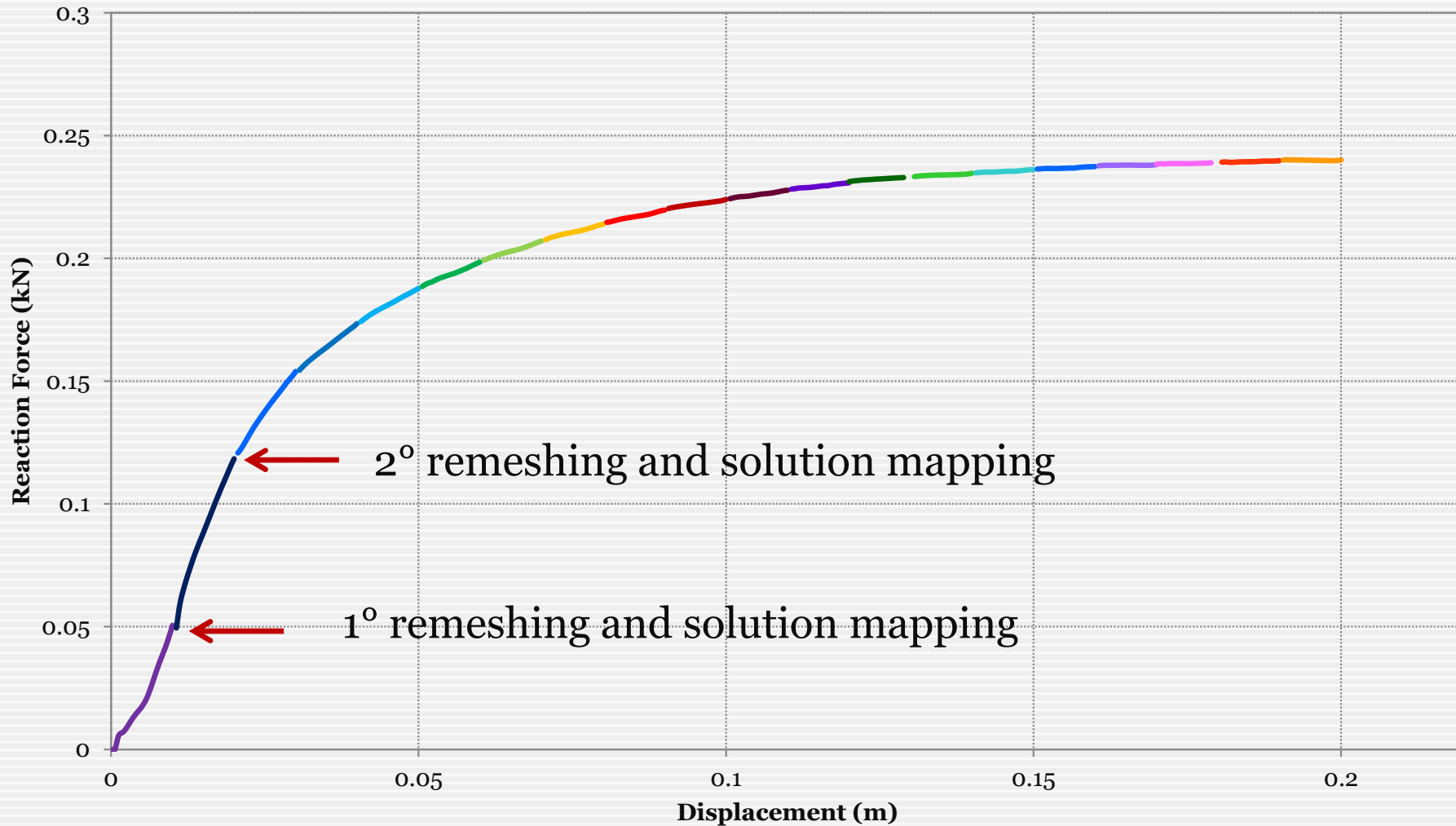
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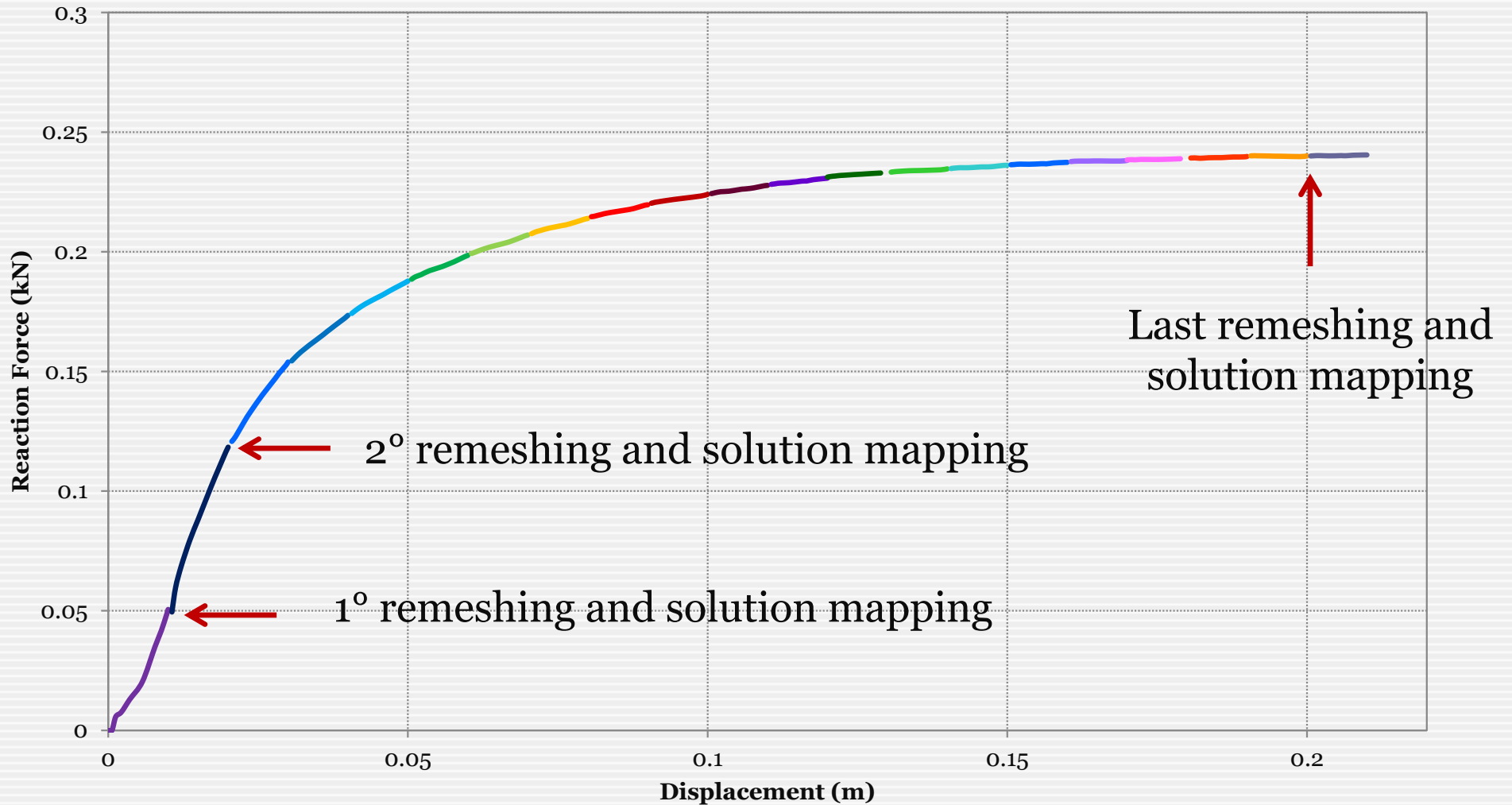
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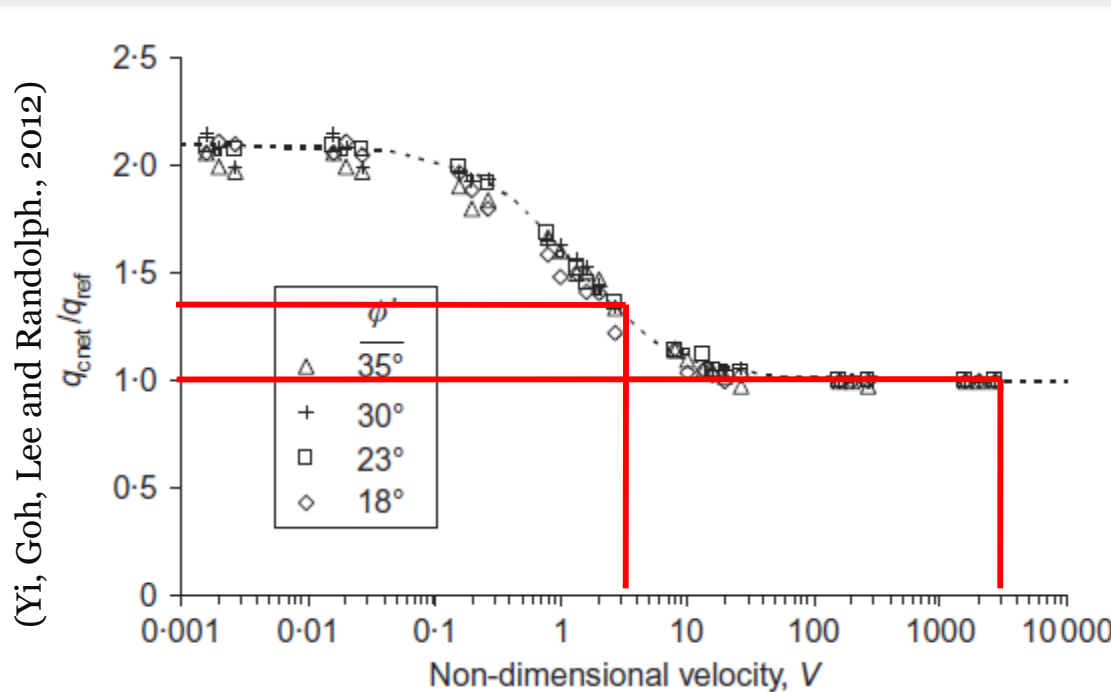
# Finite Elements analyses of cone penetration



$$D' = \frac{2G(1 - \nu')}{(1 - 2\nu')}$$

$$c_v = \frac{k}{m_v \gamma_w} = \frac{k D'}{\gamma_w}$$

Hydraulic conductivity $k$ (m/s)	$D'$ (kPa)	Penetration rate $v$ (m/s)	$c_v$ (m <sup>2</sup> /s)	$V$	$q_{cnet}/q_{ref}$
1.E-06	2880	0.02	2.9E-04	2.5E+00	1.3
1.E-09			2.9E-07	2.5E+03	1.0

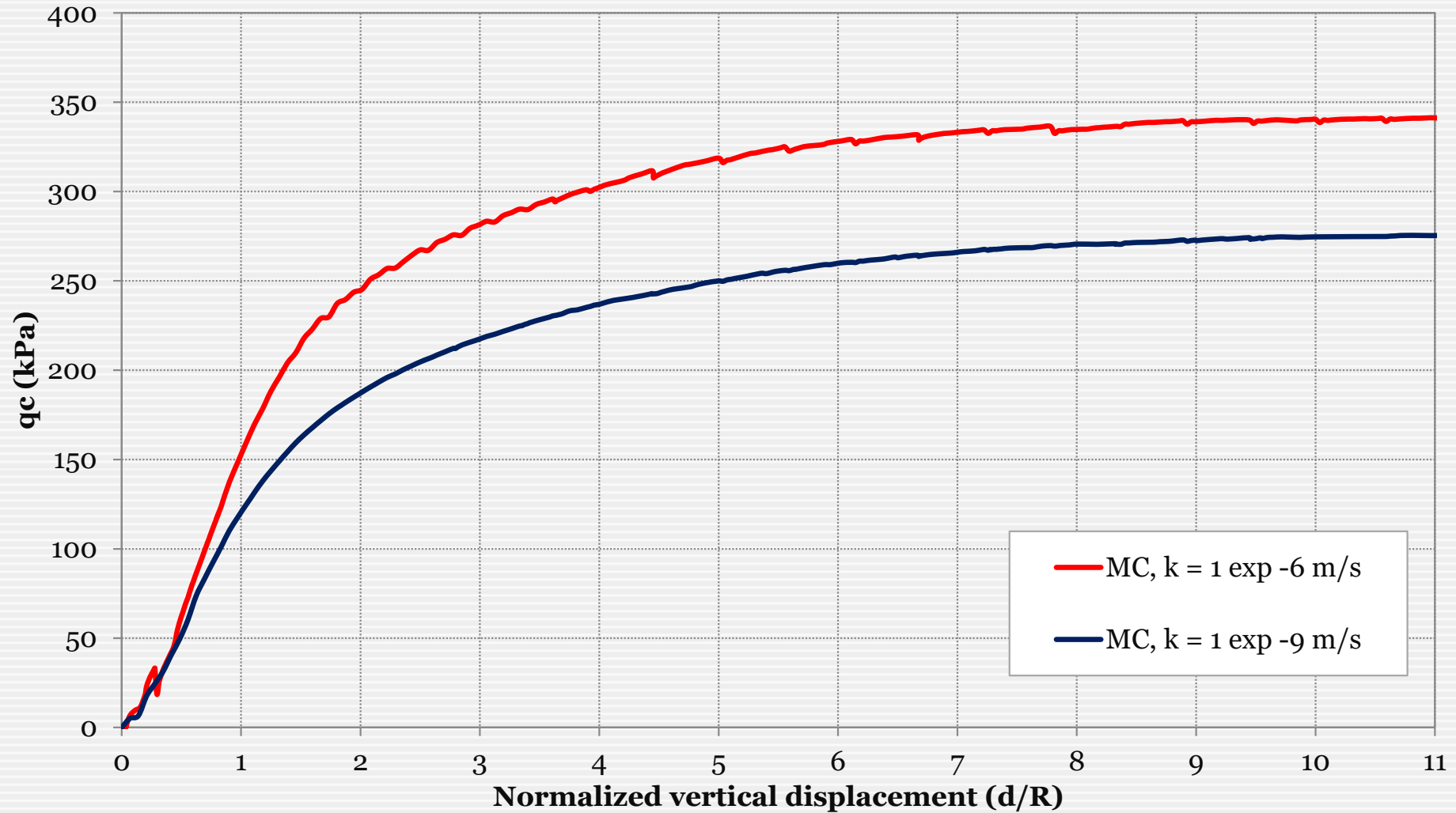


“Following Randolph & Hope (2004), the normalized cone resistance  $q_{cnet}/q_{ref}$  is defined as the net cone resistance normalized by the reference (or undrained) net cone resistance.”

$$V = \frac{v d}{c_v}$$



# Finite Elements analyses of cone penetration



# Finite Elements analyses of cone penetration



- This study represents the first step to develop a methodology aimed at simulating the large strain penetration process under different drainage conditions. For this purpose the Updated Lagrangian technique will be used for coupled-consolidation analysis, adopting more complex constitutive models for the soil
- Laboratory characterization and in situ testing of dredged sediments from the port of Livorno is currently underway. These data will be used to investigate the robustness of proposed classification schemes and will provide data for evaluating predictive capabilities of the numerical analyses.

