

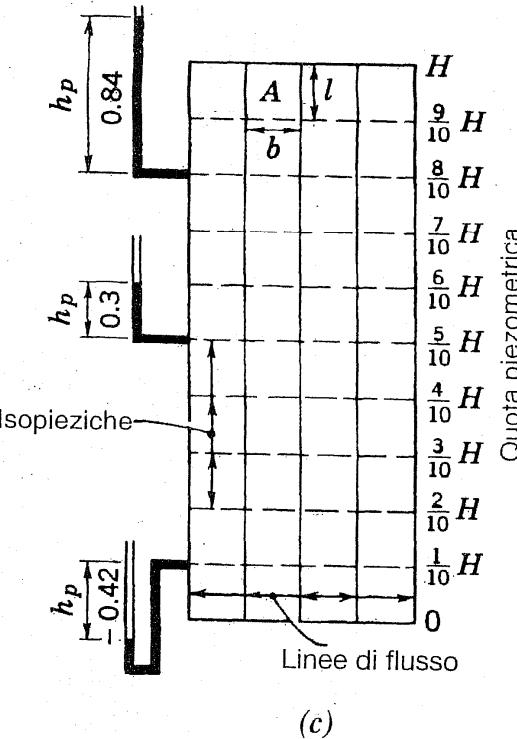
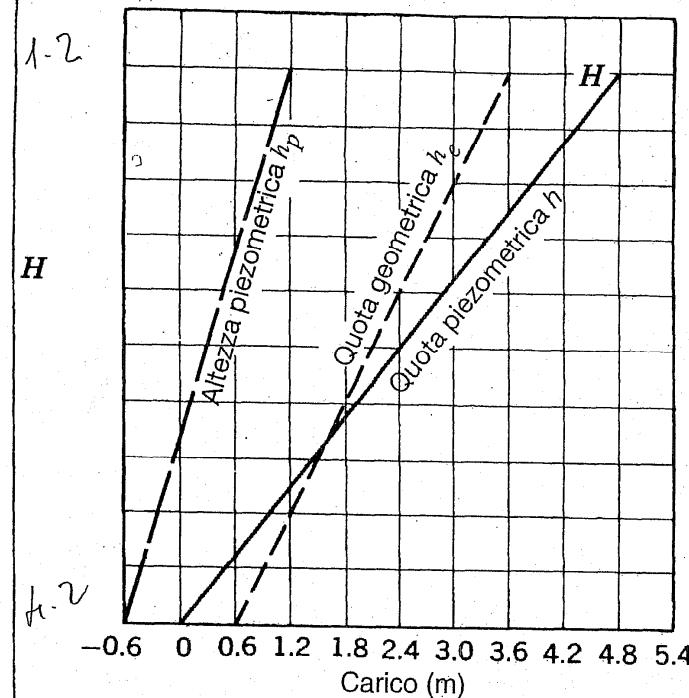
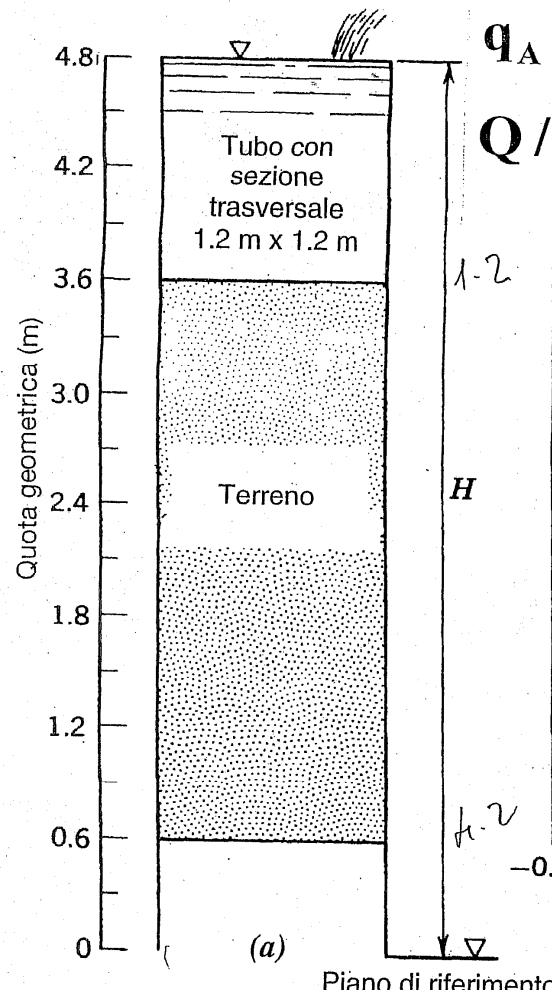
IDRAULICA: FLUSSO STAZIONARIO

MOTO DI FILTRAZIONE MONODIMENSIONALE

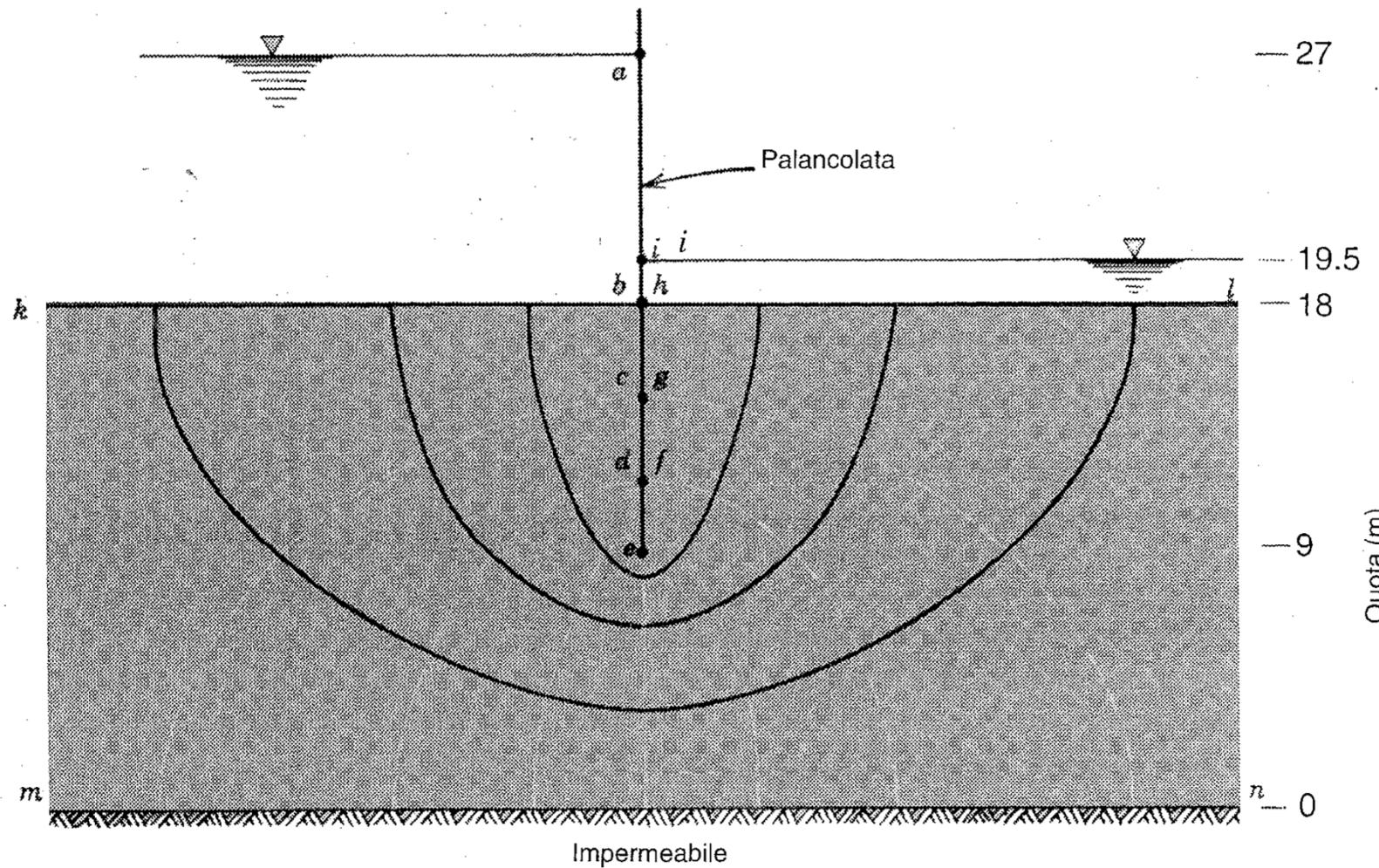
$$Q = k i A \quad (k = 0.05 \cdot 10^{-2} \text{ m/s}) \quad A = 1.2 \times 1.2$$

$$q_A = k \cdot i_A \cdot a_A = k \cdot H \cdot b / n_d l \quad (\text{portata per } L=1.0 \text{ m})$$

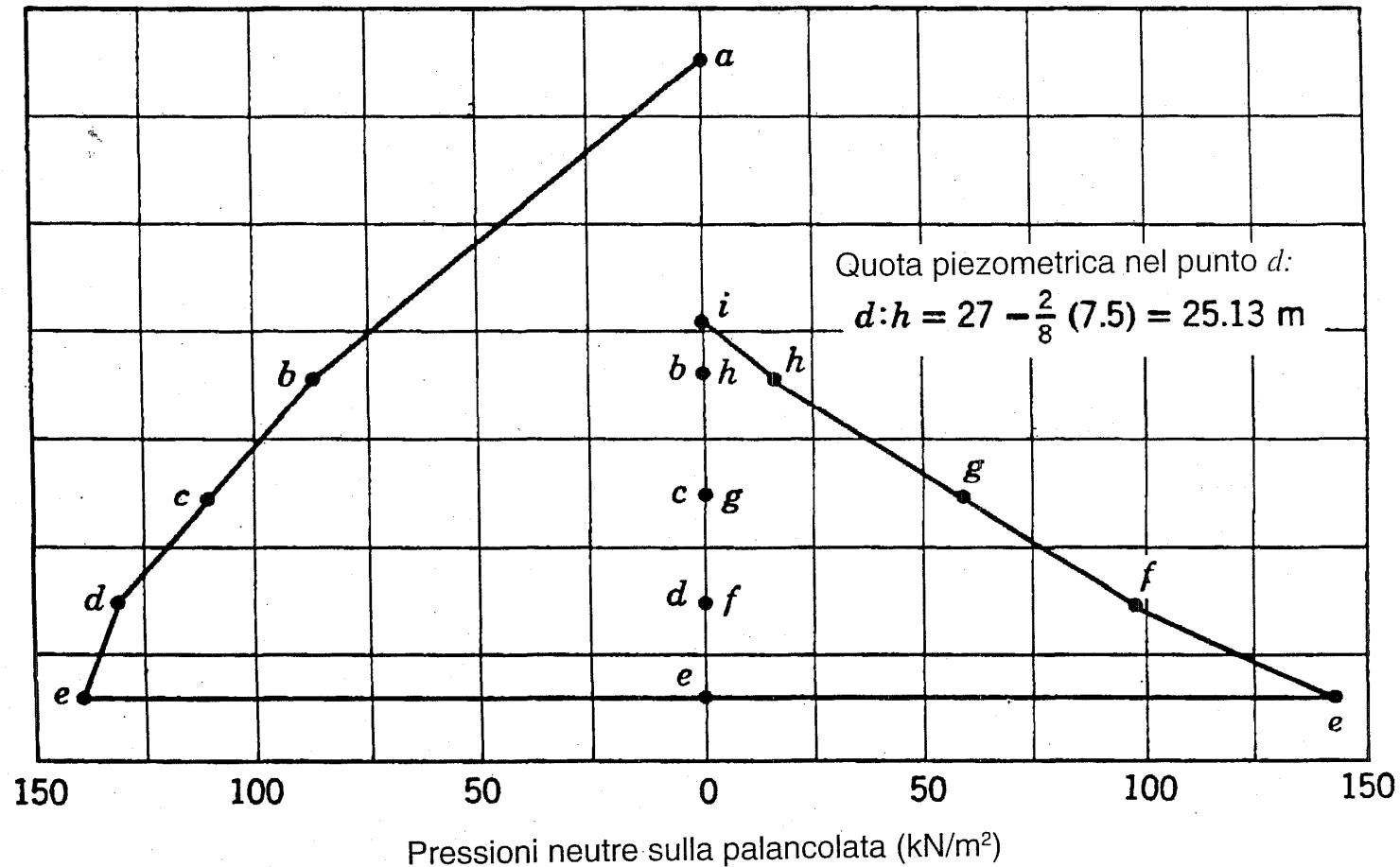
$$Q/L = q_A \cdot n_f = k \frac{n_f}{n_d} H \quad FF = n_f / n_d$$



MOTO DI FILTRAZIONE PIANO



MOTO DI FILTRAZIONE PIANO



EQUAZIONE DI FLUSSO (1)

IPOTESI:

- Interazione tra le fasi (sforzi efficaci)
- Continuità (conservazione della massa)
- Equazione di stato (densità del fluido)
- Equilibrio dinamico (Darcy)

$$q = q_x + q_y + q_z$$

$$q_z$$

$$\text{IN} \quad K_z \cdot \left(-\frac{\partial h}{\partial z} \right) \cdot dx \cdot dy$$

$$\text{OUT} \quad \left(K_z + \frac{\partial K_z}{\partial z} \cdot dz \right) \left(-\frac{\partial h}{\partial z} - \frac{\partial^2 h}{\partial z^2} dz \right) \cdot dx \cdot dy$$

Massa ($\rho_w \cdot v_i$)

equilibrio ($v_i = K_i \cdot \frac{\partial h}{\partial i}$)

permeabilità costante ($K_z = \text{costante}$)

$$\Delta q_z = \left(K_z \frac{\partial^2 h}{\partial z^2} \right) \cdot dx \cdot dy \cdot dz$$

EQUAZIONE DI FLUSSO (2)

Volume d'acqua

$$V_w = \frac{S \cdot e}{1+e} dx \cdot dy \cdot dz$$

$$\Delta q = \frac{\partial V_w}{\partial t} = \frac{\partial}{\partial t} \left(\frac{S \cdot e}{1+e} dx \cdot dy \cdot dz \right)$$

$$\Delta q = \frac{dx \cdot dy \cdot dz}{1+e} \frac{\partial S \cdot e}{\partial t}$$

$$\left(K_z \frac{\partial^2 h}{\partial z^2} + K_x \frac{\partial^2 h}{\partial x^2} \right) \cdot dx \cdot dy \cdot dz = \frac{dx \cdot dy \cdot dz}{1+e} \frac{\partial S \cdot e}{\partial t}$$

$$K_z \frac{\partial^2 h}{\partial z^2} + K_x \frac{\partial^2 h}{\partial x^2} = \frac{1}{1+e} \left(e \frac{\partial S}{\partial t} + S \frac{\partial e}{\partial t} \right)$$

a) e, S costanti

b) e varia S costante

c) e costante S varia

d) e, S variano

filtrazione

consolidazione

drenaggio/imbibizione

$$K_z \frac{\partial^2 h}{\partial z^2} + K_x \frac{\partial^2 h}{\partial x^2} = 0$$

$$\frac{\partial^2 h}{\partial z^2} + \frac{\partial^2 h}{\partial x^2} = 0$$

SOLUZIONE DELL'EQUAZIONE DI LAPLACE

Sviluppo in serie di Taylor

$$f(x) = f(x_0) + f'(x_0) \cdot (x - x_0) + \frac{f''(x_0)}{2!} \cdot (x - x_0)^2 + \frac{f'''(x_0)}{3!} \cdot (x - x_0)^3$$

$$h_1 = h_0 + \left(\frac{\partial h}{\partial x} \right)_0 \cdot \Delta x + \left(\frac{\partial^2 h}{\partial x^2} \right)_0 \cdot \frac{\Delta x^2}{2!} + \left(\frac{\partial^3 h}{\partial x^3} \right)_0 \cdot \frac{\Delta x^3}{3!} +$$

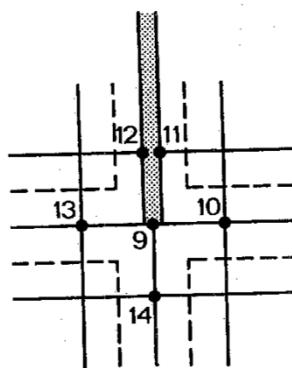
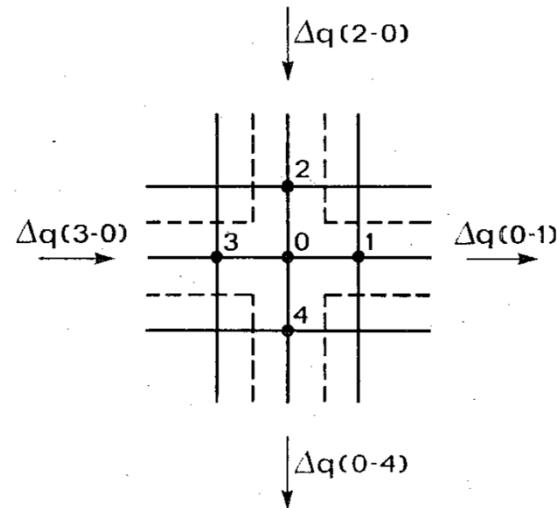
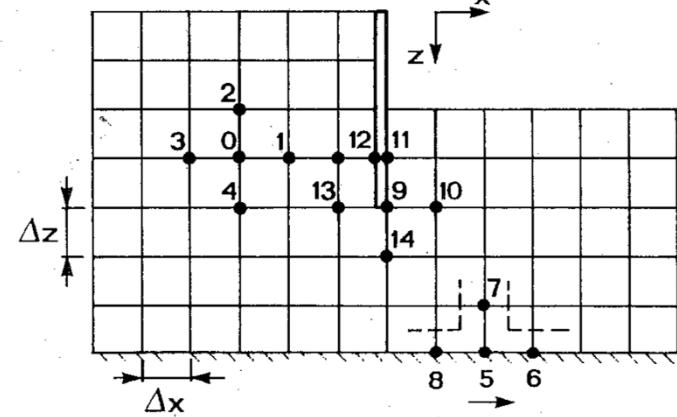
$$h_3 = h_0 - \left(\frac{\partial h}{\partial x} \right)_0 \cdot \Delta x + \left(\frac{\partial^2 h}{\partial x^2} \right)_0 \cdot \frac{\Delta x^2}{2!} - \left(\frac{\partial^3 h}{\partial x^3} \right)_0 \cdot \frac{\Delta x^3}{3!} +$$

$$\left(\frac{\partial^2 h}{\partial x^2} \right)_0 = \frac{h_1 + h_3 - 2h_0}{\Delta x^2}$$

$$\left(\frac{\partial^2 h}{\partial z^2} \right)_0 = \frac{h_2 + h_4 - 2h_0}{\Delta z^2}$$

$$\frac{h_1 + h_3 - 2h_0}{\Delta x^2} + \frac{h_2 + h_4 - 2h_0}{\Delta z^2} = 0$$

RELAZIONE DI CONTINUITÀ'



RELAZIONE DI CONTINUITA'

$$\Delta q(2-0) = K_z i \Delta x = K_z \frac{h_2 - h_o}{\Delta z} \Delta x$$

$$\Delta q(0-4) = K_z i \Delta x = K_z \frac{h_o - h_4}{\Delta z} \Delta x$$

$$\Delta q(3-0) = K_x i \Delta z = K_x \frac{h_3 - h_o}{\Delta x} \Delta z$$

$$\Delta q(0-1) = K_x i \Delta z = K_x \frac{h_o - h_1}{\Delta x} \Delta z$$

$$\left[\frac{h_8 - h_5}{\Delta x} \frac{\Delta z}{2} \right] - \left[\frac{h_5 - h_6}{\Delta x} \frac{\Delta z}{2} \right] - \left[\frac{h_5 - h_7}{\Delta z} \Delta x \right] = 0$$
$$\left[\frac{h_8}{2} \right] + \left[\frac{h_6}{2} \right] + h_7 - 2h_5 = 0$$

$$(h_{13} - h_9) - (h_9 - h_{10}) + (h_{14} - h_9) - \\ 0.5(h_9 - h_{12}) - 0.5(h_9 - h_{11}) = 0$$

MEZZO ETEROGENEO O ANISOTROPO

$$\frac{K_x}{\Delta x^2} (h_1 + h_3 - 2h_o) + \frac{K_z}{\Delta z^2} (h_2 + h_4 - 2h_o) = 0$$

$$\Delta x = \Delta z \cdot (K_x / K_z)^{0.5}$$

oppure

$$K_x \cdot \frac{\partial^2 h}{\partial x^2} + K_z \cdot \frac{\partial^2 h}{\partial z^2} = 0$$

$$y = x(K_z / K_x)^{0.5}$$

$$q = K_e i \Delta z = K_e \frac{\Delta h}{\Delta y} \Delta z$$

$$q = K_x \frac{\Delta h}{\Delta x} \Delta z = K_x \frac{\Delta h}{\Delta y (K_x / K_z)^{0.5}} \Delta z = (K_x K_z)^{0.5} \Delta h$$

MOTO NON CONFINATO

IPOTESI DI DUPUIT:

- gradiente idraulico costante in un piano V
- gradiente idraulico=pendenza
- linee di flusso orizzontali

$$q_x = K_x \cdot \left(-\frac{\partial h}{\partial x} \right) \cdot h \cdot dy$$

$$q_{x+dx} = K_x \cdot \left(-\frac{\partial h}{\partial x} \right) \cdot h \cdot dy + K_x \cdot \frac{\partial}{\partial x} \left(-h \cdot \frac{\partial h}{\partial x} \right) \cdot dx \cdot dy$$

$$\Delta q_x = K_x \cdot \frac{\partial}{\partial x} \left(h \frac{\partial h}{\partial x} \right) \cdot dx \cdot dy$$

MOTO STAZIONARIO

$$K_y \frac{\partial^2 h^2}{\partial y^2} + K_x \frac{\partial^2 h^2}{\partial x^2} = 0$$

$$\frac{\partial^2 h^2}{\partial y^2} + \frac{\partial^2 h^2}{\partial x^2} = 0$$

